

# Information Flow

## Chapter 17

# Overview

- Basics and background
  - Entropy
- Non-lattice flow policies
- Compiler-based mechanisms
- Execution-based mechanisms
- Examples
  - Privacy and cell phones
  - Firewalls

# Basics

- Bell-LaPadula Model embodies information flow policy
  - Given compartments  $A, B$ , info can flow from  $A$  to  $B$  iff  $B \text{ dom } A$
- So does Biba Model
  - Given compartments  $A, B$ , info can flow from  $A$  to  $B$  iff  $A \text{ dom } B$
- Variables  $x, y$  assigned compartments  $\underline{x}, \underline{y}$  as well as values
  - Confidentiality (Bell-LaPadula): if  $\underline{x} = A, \underline{y} = B$ , and  $B \text{ dom } A$ , then  $y := x$  allowed but not  $x := y$
  - Integrity (Biba): if  $\underline{x} = A, \underline{y} = B$ , and  $A \text{ dom } B$ , then  $x := y$  allowed but not  $y := x$
- From here on, the focus is on confidentiality (Bell-LaPadula)
  - Discuss integrity later

# Entropy and Information Flow

- Idea: info flows from  $x$  to  $y$  as a result of a sequence of commands  $c$  if you can deduce information about  $x$  before  $c$  from the value in  $y$  after  $c$
- Formally:
  - $s$  time before execution of  $c$ ,  $t$  time after
  - $H(x_s | y_t) < H(x_s | y_s)$
  - If no  $y$  at time  $s$ , then  $H(x_s | y_t) < H(x_s)$

# Example 1

- Command is  $x := y + z$ ; where:
  - $0 \leq y \leq 7$ , equal probability
  - $z = 1$  with prob.  $1/2$ ,  $z = 2$  or  $3$  with prob.  $1/4$  each
- $s$  state before command executed;  $t$ , after; so
  - $H(y_s) = H(y_t) = -8(1/8) \lg (1/8) = 3$
  - $H(z_s) = H(z_t) = -(1/2) \lg (1/2) - 2(1/4) \lg (1/4) = 1.5$
- If you know  $x_t$ ,  $y_s$  can have at most 3 values, so  $H(y_s \mid x_t) = -3(1/3) \lg (1/3) = \lg 3 \approx 1.58$ 
  - Thus, information flows from  $y$  to  $x$

# Example 2

- Command is

**if  $x = 1$  then  $y := 0$  else  $y := 1$ ;**

where  $x, y$  equally likely to be either 0 or 1

- $H(x_s) = 1$  as  $x$  can be either 0 or 1 with equal probability
- $H(x_s | y_t) = 0$  as if  $y_t = 1$  then  $x_s = 0$  and vice versa
  - Thus,  $H(x_s | y_t) = 0 < 1 = H(x_s)$
- So information flowed from  $x$  to  $y$

# Implicit Flow of Information

- Information flows from  $x$  to  $y$  without an *explicit* assignment of the form  $y := f(x)$ 
  - $f(x)$  an arithmetic expression with variable  $x$
- Example from previous slide:  
**if  $x = 1$  then  $y := 0$  else  $y := 1$ ;**
- So must look for implicit flows of information to analyze program

# Notation

- $\underline{x}$  means class of  $x$ 
  - In Bell-LaPadula based system, same as “label of security compartment to which  $x$  belongs”
- $\underline{x} \leq \underline{y}$  means “information can flow from an element in class of  $x$  to an element in class of  $y$ ”
  - Or, “information with a label placing it in class  $\underline{x}$  can flow into class  $\underline{y}$ ”



# Information Flow Policies

Information flow policies are usually:

- reflexive
  - So information can flow freely among members of a single class
- transitive
  - So if information can flow from class 1 to class 2, and from class 2 to class 3, then information can flow from class 1 to class 3

# Non-Transitive Policies

- Betty is a confidant of Anne
- Cathy is a confidant of Betty
  - With transitivity, information flows from Anne to Betty to Cathy
- Anne confides to Betty she is having an affair with Cathy's spouse
  - Transitivity undesirable in this case, probably

# Non-Lattice Transitive Policies

- 2 faculty members co-PIs on a grant
  - Equal authority; neither can overrule the other
- Grad students report to faculty members
- Undergrads report to grad students
- Information flow relation is:
  - Reflexive and transitive
- But some elements (people) have no “least upper bound” element
  - What is it for the faculty members?

# Confidentiality Policy Model

- Lattice model fails in previous 2 cases
- Generalize: policy  $I = (SC_I, \leq_I, join_I)$ :
  - $SC_I$  set of security classes
  - $\leq_I$  ordering relation on elements of  $SC_I$
  - $join_I$  function to combine two elements of  $SC_I$
- Example: Bell-LaPadula Model
  - $SC_I$  set of security compartments
  - $\leq_I$  ordering relation  $dom$
  - $join_I$  function  $lub$

# Confinement Flow Model

- $(I, O, confine, \rightarrow)$ 
  - $I = (SC_I, \leq_I, join_I)$
  - $O$  set of entities
  - $\rightarrow: O \times O$  with  $(a, b) \in \rightarrow$  (written  $a \rightarrow b$ ) iff information can flow from  $a$  to  $b$
  - for  $a \in O$ ,  $confine(a) = (a_L, a_U) \in SC_I \times SC_I$  with  $a_L \leq_I a_U$ 
    - Interpretation: for  $a \in O$ , if  $x \leq_I a_U$ , information can flow from  $x$  to  $a$ , and if  $a_L \leq_I x$ , information can flow from  $a$  to  $x$
    - So  $a_L$  lowest classification of information allowed to flow out of  $a$ , and  $a_U$  highest classification of information allowed to flow into  $a$

# Assumptions, *etc.*

- Assumes: object can change security classes
  - So, variable can take on security class of its data
- Object  $x$  has security class  $\underline{x}$  currently
- Note transitivity *not* required
- If information can flow from  $a$  to  $b$ , then  $b$  dominates  $a$  under ordering of policy  $I$ :

$$(\forall a, b \in O)[ a \rightarrow b \Rightarrow a_L \leq_I b_U ]$$

# Example 1

- $SC_l = \{ U, C, S, TS \}$ , with  $U \leq_l C$ ,  $C \leq_l S$ , and  $S \leq_l TS$
- $a, b, c \in O$ 
  - $\text{confine}(a) = [ C, C ]$
  - $\text{confine}(b) = [ S, S ]$
  - $\text{confine}(c) = [ TS, TS ]$
- Secure information flows:  $a \rightarrow b$ ,  $a \rightarrow c$ ,  $b \rightarrow c$ 
  - As  $a_L \leq_l b_U$ ,  $a_L \leq_l c_U$ ,  $b_L \leq_l c_U$
  - Transitivity holds

# Example 2

- $SC_l, \leq_l$  as in Example 1
- $x, y, z \in O$ 
  - $\text{confine}(x) = [ C, C ]$
  - $\text{confine}(y) = [ S, S ]$
  - $\text{confine}(z) = [ C, TS ]$
- Secure information flows:  $x \rightarrow y, x \rightarrow z, y \rightarrow z, z \rightarrow x, z \rightarrow y$ 
  - As  $x_L \leq_l y_U, x_L \leq_l z_U, y_L \leq_l z_U, z_L \leq_l x_U, z_L \leq_l y_U$
  - Transitivity does not hold
    - $y \rightarrow z$  and  $z \rightarrow x$ , but  $y \rightarrow x$  is false, because  $y_L \leq_l x_U$  is false



# Transitive Non-Lattice Policies

- $Q = (S_Q, \leq_Q)$  is a *quasi-ordered set* when  $\leq_Q$  is transitive and reflexive over  $S_Q$
- How to handle information flow?
  - Define a partially ordered set containing quasi-ordered set
  - Add least upper bound, greatest lower bound to partially ordered set
  - It's a lattice, so apply lattice rules!

# In Detail ...

- $\forall x \in S_Q$ : let  $f(x) = \{ y \mid y \in S_Q \wedge y \leq_Q x \}$ 
  - Define  $S_{QP} = \{ f(x) \mid x \in S_Q \}$
  - Define  $\leq_{QP} = \{ (x, y) \mid x, y \in S_Q \wedge x \subseteq y \}$ 
    - $S_{QP}$  partially ordered set under  $\leq_{QP}$
    - $f$  preserves order, so  $y \leq_Q x$  iff  $f(x) \leq_{QP} f(y)$
- Add upper, lower bounds
  - $S_{QP}' = S_{QP} \cup \{ S_Q, \emptyset \}$
  - Upper bound  $ub(x, y) = \{ z \mid z \in S_{QP} \wedge x \subseteq z \wedge y \subseteq z \}$
  - Least upper bound  $lub(x, y) = \bigcap ub(x, y)$ 
    - Lower bound, greatest lower bound defined analogously

# And the Policy Is ...

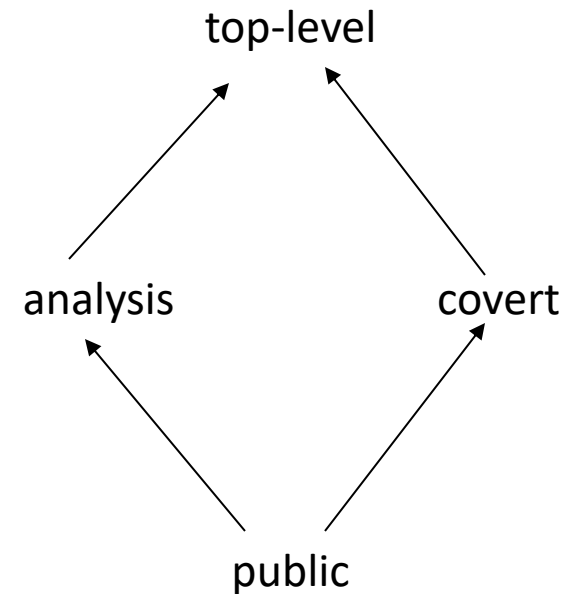
- Now  $(S_{QP'}, \leq_{QP})$  is lattice
- Information flow policy on quasi-ordered set emulates that of this lattice!

# Nontransitive Flow Policies

- Government agency information flow policy (on next slide)
- Entities public relations officers PRO, analysts A, spymasters S
  - *confine*(PRO) = [ public, analysis ]
  - *confine*(A) = [ analysis, top-level ]
  - *confine*(S) = [ covert, top-level ]

# Information Flow

- By confinement flow model:
  - $PRO \leq A, A \leq PRO$
  - $PRO \leq S$
  - $A \leq S, S \leq A$
- Data *cannot* flow to public relations officers; not transitive
  - $S \leq A, A \leq PRO$
  - $S \leq PRO$  is *false*



# Transforming Into Lattice

- Rough idea: apply a special mapping to generate a subset of the power set of the set of classes
  - Done so this set is partially ordered
  - Means it can be transformed into a lattice
- Can show this mapping preserves ordering relation
  - So it preserves non-orderings and non-transitivity of elements corresponding to those of original set

# Dual Mapping

- $R = (SC_R, \leq_R, join_R)$  reflexive info flow policy
- $P = (S_P, \leq_P)$  ordered set
  - Define *dual mapping* functions  $l_R, h_R: SC_R \rightarrow S_P$ 
    - $l_R(x) = \{x\}$
    - $h_R(x) = \{y \mid y \in SC_R \wedge y \leq_R x\}$
  - $S_P$  contains subsets of  $SC_R$ ;  $\leq_P$  subset relation
  - Dual mapping function *order preserving* iff
 
$$(\forall a, b \in SC_R) [ a \leq_R b \Leftrightarrow l_R(a) \leq_P h_R(b) ]$$

# Theorem

Dual mapping from reflexive information flow policy  $R$  to ordered set  $P$   
 order-preserving

*Proof sketch:* all notation as before

$(\Rightarrow)$  Let  $a \leq_R b$ . Then  $a \in l_R(a)$ ,  $a \in h_R(b)$ , so  $l_R(a) \subseteq h_R(b)$ , or  $l_R(a) \leq_P h_R(b)$

$(\Leftarrow)$  Let  $l_R(a) \leq_P h_R(b)$ . Then  $l_R(a) \subseteq h_R(b)$ . But  $l_R(a) = \{ a \}$ , so  $a \in h_R(b)$ ,  
 giving  $a \leq_R b$



# Information Flow Requirements

- Interpretation: let  $confine(x) = [ \underline{x}_L, \underline{x}_U ]$ , consider class  $\underline{y}$ 
  - Information can flow from  $x$  to element of  $\underline{y}$  iff  $\underline{x}_L \preceq_R \underline{y}$ , or  $I_R(\underline{x}_L) \subseteq h_R(\underline{y})$
  - Information can flow from element of  $\underline{y}$  to  $x$  iff  $\underline{y} \preceq_R \underline{x}_U$ , or  $I_R(\underline{y}) \subseteq h_R(\underline{x}_U)$

# Revisit Government Example

- Information flow policy is  $R$
- Flow relationships among classes are:

public  $\leq_R$  public

public  $\leq_R$  analysis

public  $\leq_R$  covert

public  $\leq_R$  top-level

analysis  $\leq_R$  top-level

analysis  $\leq_R$  analysis

covert  $\leq_R$  covert

covert  $\leq_R$  top-level

top-level  $\leq_R$  top-level

# Dual Mapping of $R$

- Elements  $l_R, h_R$ :

$$l_R(\text{public}) = \{ \text{public} \}$$

$$h_R(\text{public}) = \{ \text{public} \}$$

$$l_R(\text{analysis}) = \{ \text{analysis} \}$$

$$h_R(\text{analysis}) = \{ \text{public}, \text{analysis} \}$$

$$l_R(\text{covert}) = \{ \text{covert} \}$$

$$h_R(\text{covert}) = \{ \text{public}, \text{covert} \}$$

$$l_R(\text{top-level}) = \{ \text{top-level} \}$$

$$h_R(\text{top-level}) = \{ \text{public}, \text{analysis}, \text{covert}, \text{top-level} \}$$

# *confine*

- Let  $p$  be entity of type PRO,  $a$  of type A,  $s$  of type S
- In terms of  $P$  (not  $R$ ), we get:
  - $confine(p) = [ \{ public \}, \{ public, analysis \} ]$
  - $confine(a) = [ \{ analysis \}, \{ public, analysis, covert, top-level \} ]$
  - $confine(s) = [ \{ covert \}, \{ public, analysis, covert, top-level \} ]$

# And the Flow Relations Are ...

- $p \rightarrow a$  as  $I_R(p) \subseteq h_R(a)$ 
  - $I_R(p) = \{ \text{public} \}$
  - $h_R(a) = \{ \text{public, analysis, covert, top-level} \}$
- Similarly:  $a \rightarrow p, p \rightarrow s, a \rightarrow s, s \rightarrow a$
- But  $s \rightarrow p$  is false as  $I_R(s) \not\subseteq h_R(p)$ 
  - $I_R(s) = \{ \text{covert} \}$
  - $h_R(p) = \{ \text{public, analysis} \}$

# Analysis

- $(S_p, \leq_p)$  is a lattice, so it can be analyzed like a lattice policy
- Dual mapping preserves ordering, hence non-ordering and non-transitivity, of original policy
  - So results of analysis of  $(S_p, \leq_p)$  can be mapped back into  $(SC_R, \leq_R, join_R)$

# Compiler-Based Mechanisms

- Detect unauthorized information flows in a program during compilation
- Analysis not precise, but secure
  - If a flow *could* violate policy (but may not), it is unauthorized
  - No unauthorized path along which information could flow remains undetected
- Set of statements *certified* with respect to information flow policy if flows in set of statements do not violate that policy

# Example

```
if  $x = 1$  then  $y := a$ ;
```

```
else  $y := b$ ;
```

- Information flows from  $x$  and  $a$  to  $y$ , or from  $x$  and  $b$  to  $y$
- Certified only if  $\underline{x} \leq \underline{y}$  and  $\underline{a} \leq \underline{y}$  and  $\underline{b} \leq \underline{y}$ 
  - Note flows for *both* branches must be true unless compiler can determine that one branch will *never* be taken



# Declarations

- Notation:

**$x$ : int class { A, B }**

means  $x$  is an integer variable with security class at least  $lub\{ A, B \}$ , so  
 $lub\{ A, B \} \leq \underline{x}$

- Distinguished classes *Low*, *High*
  - Constants are always *Low*

# Input Parameters

- Parameters through which data passed into procedure
- Class of parameter is class of actual argument

$i_p$ : **type class** {  $i_p$  }

# Output Parameters

- Parameters through which data passed out of procedure
  - If data passed in, called input/output parameter
- As information can flow from input parameters to output parameters, class must include this:

$$o_p: \text{type class } \{ r_1, \dots, r_n \}$$

where  $r_i$  is class of  $i$ th input or input/output argument

# Example

```
proc sum(x: int class { A };  
    var out: int class { A, B } );  
begin  
    out := out + x;  
end;
```

- Require  $\underline{x} \leq \underline{out}$  and  $\underline{out} \leq \underline{out}$

# Array Elements

- Information flowing out:

$$\dots := a[i]$$

Value of  $i$ ,  $a[i]$  both affect result, so class is  $\text{lub}\{ \underline{a[i]}, \underline{i} \}$

- Information flowing in:

$$a[i] := \dots$$

- Only value of  $a[i]$  affected, so class is  $\underline{a[i]}$

# Assignment Statements

$x := y + z;$

- Information flows from  $y, z$  to  $x$ , so this requires  $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$

More generally:

$y := f(x_1, \dots, x_n)$

- the relation  $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq \underline{y}$  must hold

# Compound Statements

$x := y + z; a := b * c - x;$

- First statement:  $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$
- Second statement:  $\text{lub}\{ \underline{b}, \underline{c}, \underline{x} \} \leq \underline{a}$
- So, both must hold (i.e., be secure)

More generally:

$S_1; \dots; S_n;$

- Each individual  $S_i$  must be secure

# Conditional Statements

`if  $x + y < z$  then  $a := b$  else  $d := b * c - x$ ; end`

- Statement executed reveals information about  $x, y, z$ , so  $\text{lub}\{\underline{x}, \underline{y}, \underline{z}\} \leq \text{glb}\{\underline{a}, \underline{d}\}$

More generally:

`if  $f(x_1, \dots, x_n)$  then  $S_1$  else  $S_2$ ; end`

- $S_1, S_2$  must be secure
- $\text{lub}\{\underline{x}_1, \dots, \underline{x}_n\} \leq \text{glb}\{\underline{y} \mid y \text{ target of assignment in } S_1, S_2\}$



# Iterative Statements

```
while  $i < n$  do begin  $a[i] := b[i]; i := i + 1;$  end
```

- Same ideas as for “if”, but must terminate

More generally:

```
while  $f(x_1, \dots, x_n)$  do  $S;$ 
```

- Loop must terminate;
- $S$  must be secure
- $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq \text{glb}\{ \underline{y} \mid y \text{ target of assignment in } S \}$

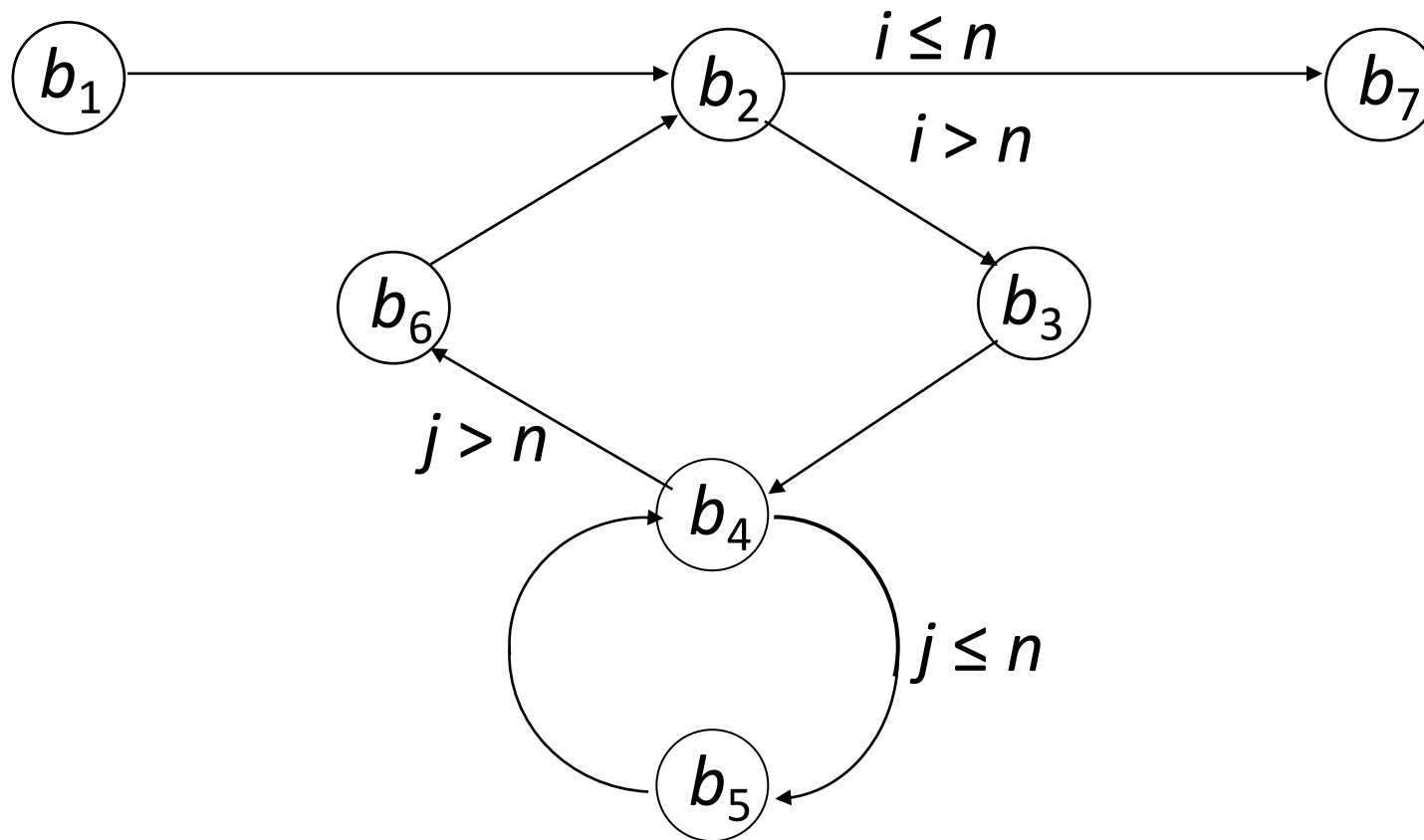
# Goto Statements

- No assignments
  - Hence no explicit flows
- Need to detect implicit flows
- *Basic block* is sequence of statements that have one entry point and one exit point
  - Control in block *always* flows from entry point to exit point

# Example Program

```
proc tm(x: array[1..10][1..10] of integer class {x};  
        var y: array[1..10][1..10] of integer class {y});  
var i, j: integer class {i};  
begin  
b1    i := 1;  
b2 L2: if i > 10 goto L7;  
b3    j := 1;  
b4 L4: if j > 10 then goto L6;  
b5    y[j][i] := x[i][j]; j := j + 1; goto L4;  
b6 L6: i := i + 1; goto L2;  
b7 L7:  
end;
```

# Flow of Control



# IFDs

- Idea: when two paths out of basic block, implicit flow occurs
  - Because information says *which* path to take
- When paths converge, either:
  - Implicit flow becomes irrelevant; or
  - Implicit flow becomes explicit
- *Immediate forward dominator* of basic block  $b$  (written  $IFD(b)$ ) is first basic block lying on all paths of execution passing through  $b$

# IFD Example

- In previous procedure:
  - $\text{IFD}(b_1) = b_2$  one path
  - $\text{IFD}(b_2) = b_7$   $b_2 \rightarrow b_7$  or  $b_2 \rightarrow b_3 \rightarrow b_6 \rightarrow b_2 \rightarrow b_7$
  - $\text{IFD}(b_3) = b_4$  one path
  - $\text{IFD}(b_4) = b_6$   $b_4 \rightarrow b_6$  or  $b_4 \rightarrow b_5 \rightarrow b_6$
  - $\text{IFD}(b_5) = b_4$  one path
  - $\text{IFD}(b_6) = b_2$  one path

# Requirements

- $B_i$  is set of basic blocks along an execution path from  $b_i$  to  $\text{IFD}(b_i)$ 
  - Analogous to statements in conditional statement
- $x_{i1}, \dots, x_{in}$  variables in expression selecting which execution path containing basic blocks in  $B_i$  used
  - Analogous to conditional expression
- Requirements for secure:
  - All statements in each basic blocks are secure
  - $\text{lub}\{ \underline{x}_{i1}, \dots, \underline{x}_{in} \} \leq \text{glb}\{ \underline{y} \mid y \text{ target of assignment in } B_i \}$

# Example of Requirements

- Within each basic block:

$$b_1: Low \leq \underline{i} \quad b_3: Low \leq \underline{j} \quad b_6: \text{lub}\{ Low, \underline{i} \} \leq \underline{i}$$

$$b_5: \text{lub}\{ \underline{x}[\underline{i}][\underline{j}], \underline{i}, \underline{j} \} \leq \underline{y}[\underline{j}][\underline{i}]; \text{lub}\{ Low, \underline{i} \} \leq \underline{j}$$

- Combining,  $\text{lub}\{ \underline{x}[\underline{i}][\underline{j}], \underline{i}, \underline{j} \} \leq \underline{y}[\underline{j}][\underline{i}]$
- From declarations, true when  $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$
- $B_2 = \{b_3, b_4, b_5, b_6\}$ 
  - Assignments to  $i, j, y[j][i]$ ; conditional is  $i \leq 10$
  - Requires  $\underline{i} \leq \text{glb}\{ \underline{i}, \underline{j}, \underline{y}[\underline{j}][\underline{i}] \}$
  - From declarations, true when  $\underline{i} \leq \underline{y}$



# Example (continued)

- $B_4 = \{ b_5 \}$ 
  - Assignments to  $j, y[j][i]$ ; conditional is  $j \leq 10$
  - Requires  $\underline{j} \leq \text{glb}\{ \underline{j}, \underline{y}[\underline{j}][\underline{i}] \}$
  - From declarations, means  $\underline{j} \leq \underline{y}$
- Result:
  - Combine  $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}; \underline{i} \leq \underline{y}; \underline{i} \leq \underline{y}$
  - Requirement is  $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$

# Procedure Calls

$tm(a, b);$

From previous slides, to be secure,  $\text{lub}\{\underline{x}, \underline{i}\} \leq \underline{y}$  must hold

- In call,  $x$  corresponds to  $a$ ,  $y$  to  $b$
- Means that  $\text{lub}\{\underline{a}, \underline{i}\} \leq \underline{b}$ , or  $\underline{a} \leq \underline{b}$

More generally:

**proc**  $pn(i_1, \dots, i_m: \mathbf{int}; \mathbf{var} \ o_1, \dots, o_n: \mathbf{int}); \mathbf{begin} \ S \ \mathbf{end};$

- $S$  must be secure
- For all  $j$  and  $k$ , if  $\underline{i}_j \leq \underline{o}_k$ , then  $\underline{x}_j \leq \underline{y}_k$
- For all  $j$  and  $k$ , if  $\underline{o}_j \leq \underline{o}_k$ , then  $\underline{y}_j \leq \underline{y}_k$

# Exceptions

```
proc copy(x: integer class { x };  
           var y: integer class Low);  
var sum: integer class { x };  
    z: int class Low;  
begin  
    y := z := sum := 0;  
    while z = 0 do begin  
        sum := sum + x;  
        y := y + 1;  
    end  
end
```

# Exceptions (*cont*)

- When sum overflows, integer overflow trap
  - Procedure exits
  - Value of  $x$  is  $\text{MAXINT}/y$
  - Information flows from  $y$  to  $x$ , but  $\underline{x} \leq \underline{y}$  never checked

- Need to handle exceptions explicitly

- Idea: on integer overflow, terminate loop

**on integer\_overflow\_exception *sum* do  $z := 1;$**

- Now information flows from  $sum$  to  $z$ , meaning  $\underline{sum} \leq \underline{z}$
- This is false ( $\underline{sum} = \{x\}$  dominates  $\underline{z} = \text{Low}$ )

# Infinite Loops

```
proc copy(x: integer 0..1 class { x };  
          var y: integer 0..1 class Low);  
begin  
    y := 0;  
    while x = 0 do  
        (* nothing *);  
    y := 1;  
end
```

- If  $x = 0$  initially, infinite loop
- If  $x = 1$  initially, terminates with  $y$  set to 1
- No explicit flows, but implicit flow from  $x$  to  $y$

# Semaphores

Use these constructs:

**wait**( $x$ ):    **if**  $x = 0$  **then block until**  $x > 0$ ;  $x := x - 1$ ;

**signal**( $x$ ):  $x := x + 1$ ;

- $x$  is semaphore, a shared variable
- Both executed atomically

Consider statement

`wait(sem);  $x := x + 1$ ;`

- Implicit flow from *sem* to  $x$ 
  - Certification must take this into account!

# Flow Requirements

- Semaphores in *signal* irrelevant
  - Don't affect information flow in that process
- Statement  $S$  is a *wait*
  - $\text{shared}(S)$ : set of shared variables read
    - Idea: information flows out of variables in  $\text{shared}(S)$
  - $\text{fglb}(S)$ : glb of assignment targets *following*  $S$
  - So, requirement is  $\text{shared}(S) \leq \text{fglb}(S)$
- $\text{begin } S_1; \dots S_n \text{ end}$ 
  - All  $S_i$  must be secure
  - For all  $i$ ,  $\text{shared}(S_i)$   $\leq \text{fglb}(S_i)$

# Example

**begin**

$x := y + z;$        $( * S_1 * )$

**wait**( $sem$ );       $( * S_2 * )$

$a := b * c - x;$        $( * S_3 * )$

**end**

- Requirements:

- $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$

- $\text{lub}\{ \underline{b}, \underline{c}, \underline{x} \} \leq \underline{a}$

- $\underline{sem} \leq \underline{a}$

- Because  $\text{fglb}(S_2) = \underline{a}$  and  $\text{shared}(S_2) = sem$



# Concurrent Loops

- Similar, but wait in loop affects *all* statements in loop
  - Because if flow of control loops, statements in loop before wait may be executed after wait
- Requirements
  - Loop terminates
  - All statements  $S_1, \dots, S_n$  in loop secure
  - $\text{lub}\{ \underline{\text{shared}}(S_1), \dots, \underline{\text{shared}}(S_n) \} \leq \text{glb}(t_1, \dots, t_m)$ 
    - Where  $t_1, \dots, t_m$  are variables assigned to in loop

# Loop Example

**while**  $i < n$  **do begin**

$a[i] := item;$        $( * S_1 * )$

**wait**( $sem$ );       $( * S_2 * )$

$i := i + 1;$        $( * S_3 * )$

**end**

- Conditions for this to be secure:
  - Loop terminates, so this condition met
  - $S_1$  secure if  $\text{lub}\{ \underline{i}, \underline{item} \} \leq \underline{a[i]}$
  - $S_2$  secure if  $\underline{sem} \leq \underline{i}$  and  $\underline{sem} \leq \underline{a[i]}$
  - $S_3$  trivially secure

# *cobegin/coend*

## **cobegin**

$$x := y + z; \quad (* S_1 *)$$

$$a := b * c - y; \quad (* S_2 *)$$

## **coend**

- No information flow among statements
  - For  $S_1$ ,  $\text{lub}\{\underline{y}, \underline{z}\} \leq \underline{x}$
  - For  $S_2$ ,  $\text{lub}\{\underline{b}, \underline{c}, \underline{y}\} \leq \underline{a}$
- Security requirement is both must hold
  - So this is secure if  $\text{lub}\{\underline{y}, \underline{z}\} \leq \underline{x} \wedge \text{lub}\{\underline{b}, \underline{c}, \underline{y}\} \leq \underline{a}$

# Soundness

- Above exposition intuitive
- Can be made rigorous:
  - Express flows as types
  - Equate certification to correct use of types
  - Checking for valid information flows same as checking types conform to semantics imposed by security policy

# Execution-Based Mechanisms

- Detect and stop flows of information that violate policy
  - Done at run time, not compile time
- Obvious approach: check explicit flows
  - Problem: assume for security,  $\underline{x} \leq \underline{y}$   
**if  $x = 1$  then  $y := a$ ;**
  - When  $x \neq 1$ ,  $\underline{x} = \text{High}$ ,  $\underline{y} = \text{Low}$ ,  $\underline{a} = \text{Low}$ , appears okay—but implicit flow violates condition!

# Fenton's Data Mark Machine

- Each variable has an associated class
- Program counter (PC) has one too
- Idea: branches are assignments to PC, so you can treat implicit flows as explicit flows
- Stack-based machine, so everything done in terms of pushing onto and popping from a program stack

# Instruction Description

- *skip* means instruction not executed
- *push*( $x, \underline{x}$ ) means push variable  $x$  and its security class  $\underline{x}$  onto program stack
- *pop*( $x, \underline{x}$ ) means pop top value and security class from program stack, assign them to variable  $x$  and its security class  $\underline{x}$  respectively

# Instructions

- $x := x + 1$  (increment)
  - Same as:
 

```
if PC ≤ x then  $x := x + 1$  else skip
```
- **if**  $x = 0$  **then goto**  $n$  **else**  $x := x - 1$  (branch and save PC on stack)
  - Same as:
 

```
if  $x = 0$  then begin  

            push( $PC$ , PC); PC :=  $\text{lub}\{\text{PC}, x\}$ ;  $PC := n$ ;  

            end else if PC ≤ x then  

               $x := x - 1$   

else  

            skip;
```



# More Instructions

- **if'  $x = 0$  then goto  $n$  else  $x := x - 1$**  (branch without saving PC on stack)

- Same as:

```
if  $x = 0$  then
```

```
    if  $\underline{x} \leq \underline{PC}$  then  $PC := n$  else skip
```

```
else
```

```
    if  $\underline{PC} \leq \underline{x}$  then  $x := x - 1$  else skip
```

# More Instructions

- **return** (go to just after last *if*)
  - Same as:  
**pop** (*PC*, *PC*);
- **halt** (stop)
  - Same as:  
**if** *program stack empty* **then** *halt*
  - Note stack empty to prevent user obtaining information from it after halting

# Example Program

```
1  if  $x = 0$  then goto 4 else  $x := x - 1$   
2  if  $z = 0$  then goto 6 else  $z := z - 1$   
3  halt  
4   $z := z - 1$   
5  return  
6   $y := y - 1$   
7  return
```

Initially  $x = 0$  or  $x = 1$ ,  $y = 0$ ,  $z = 0$

Program copies value of  $x$  to  $y$

# Example Execution

<i>x</i>	<i>y</i>	<i>z</i>	<i>PC</i>	<u><i>PC</i></u>	<i>stack</i>	<i>check</i>
1	0	0	1	Low	—	
0	0	0	2	Low	—	$\text{Low} \leq \underline{x}$
0	0	0	6	<u><i>z</i></u>	(3, Low)	<u><i>PC</i></u> $\leq$ <u><i>y</i></u>
0	1	0	7	<u><i>z</i></u>	(3, Low)	
0	1	0	3	Low	—	

# Handling Errors

- Ignore statement that causes error, but continue execution
  - If aborted or a visible exception taken, user could deduce information
  - Means errors cannot be reported unless user has clearance at least equal to that of the information causing the error

# Variable Classes

- Up to now, classes fixed
  - Check relationships on assignment, etc.
- Consider variable classes
  - Fenton's Data Mark Machine does this for PC
  - On assignment of form  $y := f(x_1, \dots, x_n)$ , y changed to  $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \}$
  - Need to consider implicit flows, also

# Example Program

```
(* Copy value from x to y. Initially, x is 0 or 1 *)
proc copy(x: integer class { x });
           var y: integer class { y })
var z: integer class variable { Low };
begin
  y := 0;
  z := 0;
  if x = 0 then z := 1;
  if z = 0 then y := 1;
end;
```

- z changes when z assigned to
- Assume y < x

# Analysis of Example

- $x = 0$ 
  - $z := 0$  sets  $\underline{z}$  to Low
  - if  $x = 0$  then  $z := 1$  sets  $z$  to 1 and  $\underline{z}$  to  $\underline{x}$
  - So on exit,  $y = 0$
- $x = 1$ 
  - $z := 0$  sets  $\underline{z}$  to Low
  - if  $z = 0$  then  $y := 1$  sets  $y$  to 1 and checks that  $\text{lub}\{\text{Low}, \underline{z}\} \leq \underline{y}$
  - So on exit,  $y = 1$
- Information flowed from  $\underline{x}$  to  $\underline{y}$  even though  $\underline{y} < \underline{x}$



# Handling This (1)

- Fenton's Data Mark Machine detects implicit flows violating certification rules

# Handling This (2)

- Raise class of variables assigned to in conditionals even when branch not taken
- Also, verify information flow requirements even when branch not taken
- Example:
  - In **if**  $x = 0$  **then**  $z := 1$ ,  $z$  raised to  $x$  whether or not  $x = 0$
  - Certification check in next statement, that  $\underline{z} \leq \underline{y}$ , fails, as  $\underline{z} = \underline{x}$  from previous statement, and  $\underline{y} \leq \underline{x}$

# Handling This (3)

- Change classes only when explicit flows occur, but *all* flows (implicit as well as explicit) force certification checks
- Example
  - When  $x = 0$ , first **if** sets  $\underline{z}$  to Low, then checks  $\underline{x} \leq \underline{z}$
  - When  $x = 1$ , first **if** checks  $\underline{x} \leq \underline{z}$
  - This holds if and only if  $\underline{x} = \text{Low}$ 
    - Not possible as  $\underline{y} < \underline{x} = \text{Low}$  by assumption and there is no such class

# Integrity Mechanisms

- The above also works with Biba, as it is mathematical dual of Bell-LaPadula
- All constraints are simply duals of confidentiality-based ones presented above

# Example 1

For information flow of assignment statement:

$$y := f(x_1, \dots, x_n)$$

the relation  $\text{glb}\{x_1, \dots, x_n\} \leq y$  must hold

- Why? Because information flows from  $x_1, \dots, x_n$  to  $y$ , and under Biba, information must flow from a higher (or equal) class to a lower one

# Example 2

For information flow of conditional statement:

**if**  $f(x_1, \dots, x_n)$  **then**  $S_1$ ; **else**  $S_2$ ; **end**;

then the following must hold:

- $S_1, S_2$  must satisfy integrity constraints
- $\text{glb}\{ \underline{x}_1, \dots, \underline{x}_n \} \geq \text{lub}\{ \underline{y} \mid y \text{ target of assignment in } S_1, S_2 \}$

# Example Information Flow Control Systems

- Use access controls of various types to inhibit information flows
- Privacy and Android Cell Phones
  - Analyzes data being sent from the phone
- Firewalls

# Privacy and Android Cell Phones

- Many commercial apps use advertising libraries to monitor clicks, fetch ads, display them
  - So they send information, ostensibly to help tailor advertising to you
- Many apps ask to have full access to phone, data
  - This is because of complexity of permission structure of Android system
- Ads displayed with privileges of app
  - And if they use Javascript, that executes with those privileges
  - So if it has full access privilege, it can send contact lists, other information to others
- Information flow problem as information is flowing from phone to external party



# Analyzing Android Flows

- Android based on Linux
  - App executables in bytecode format (Dalvik executables, or DEX) and run in Dalvik VM
  - Apps event driven
  - Apps use system libraries to do many of their functions
  - Binder subsystem controls interprocess communication
- Analysis uses 2 security levels, *untainted* and *tainted*
  - No categories, and *tainted* < *untainted*

# TaintDroid: Checking Information Flows

- All objects tagged *tainted* or *untainted*
  - Interpreters, Binder augmented to handle tags
- Android native libraries trusted
  - Those communicating externally are *taint sinks*
- When untrusted app invokes a taint sink library, taint tag of data is recorded
- Taint tags assigned to external variables, library return values
  - These are assigned based on knowledge of what native code does
- Files have single taint tag, updated when file is written
- Database queries retrieve information, so tag determined by database query responder

# TaintDroid: Checking Information Flows

- Information from phone sensor may be sensitive; if so, *tainted*
  - TaintDroid determines this from characteristics of information
- Experiment 1 (2010): select 30 popular apps out of a set of 358 that required permission to access Internet, phone location, camera, or microphone; also could access cell phone information
  - 105 network connections accessed *tainted* data
  - 2 sent phone identification information to a server
  - 9 sent device identifiers to third parties, and 2 didn't tell user
  - 15 sent location information to third parties, none told user
  - No false positives

# TaintDroid: Checking Information Flows

- Experiment 2 (2010): revisit 18 out of the 30 apps (others did not run on current version of Android)
  - 3 still sent location information to third parties
  - 8 sent device identification information to third parties without consent
    - 3 of these did so in 2010 experiment
    - 5 were new
  - 2 new flows that could reveal *tainted* data
  - No false positives

# Firewalls

- Host that mediates access to a network
  - Allows, disallows accesses based on configuration and type of access
- Example: block Conficker worm
  - Conficker connects to botnet, which can use system for many purposes
    - Spreads through a vulnerability in a particular network service
  - Firewall analyze packets using that service remotely, and look for Conficker and its variants
    - If found, packets discarded, and other actions may be taken
  - Conficker also generates list of host names, tried to contact botnets at those hosts
    - As set of domains known, firewall can also block outbound traffic to those hosts

# Filtering Firewalls

- Access control based on attributes of packets and packet headers
  - Such as destination address, port numbers, options, etc.
  - Also called a *packet filtering firewall*
  - Does not control access based on content
  - Examples: routers, other infrastructure systems

# Proxy

- Intermediate agent or server acting on behalf of endpoint without allowing a direct connection between the two endpoints
  - So each endpoint talks to proxy, thinking it is talking to other endpoint
  - Proxy decides whether to forward messages, and whether to alter them

# Proxy Firewall

- Access control done with proxies
  - Usually bases access control on content as well as source, destination addresses, etc.
  - Also called an *applications level* or *application level firewall*
  - Example: virus checking in electronic mail
    - Incoming mail goes to proxy firewall
    - Proxy firewall receives mail, scans it
    - If no virus, mail forwarded to destination
    - If virus, mail rejected or disinfected before forwarding



# Example

- Want to scan incoming email for malware
- Firewall acts as recipient, gets packets making up message and reassembles the message
  - It then scans the message for malware
  - If none, message forwarded
  - If some found, mail is discarded (or some other appropriate action)
- As email reassembled at firewall by a mail agent acting on behalf of mail agent at destination, it's a proxy firewall (application layer firewall)

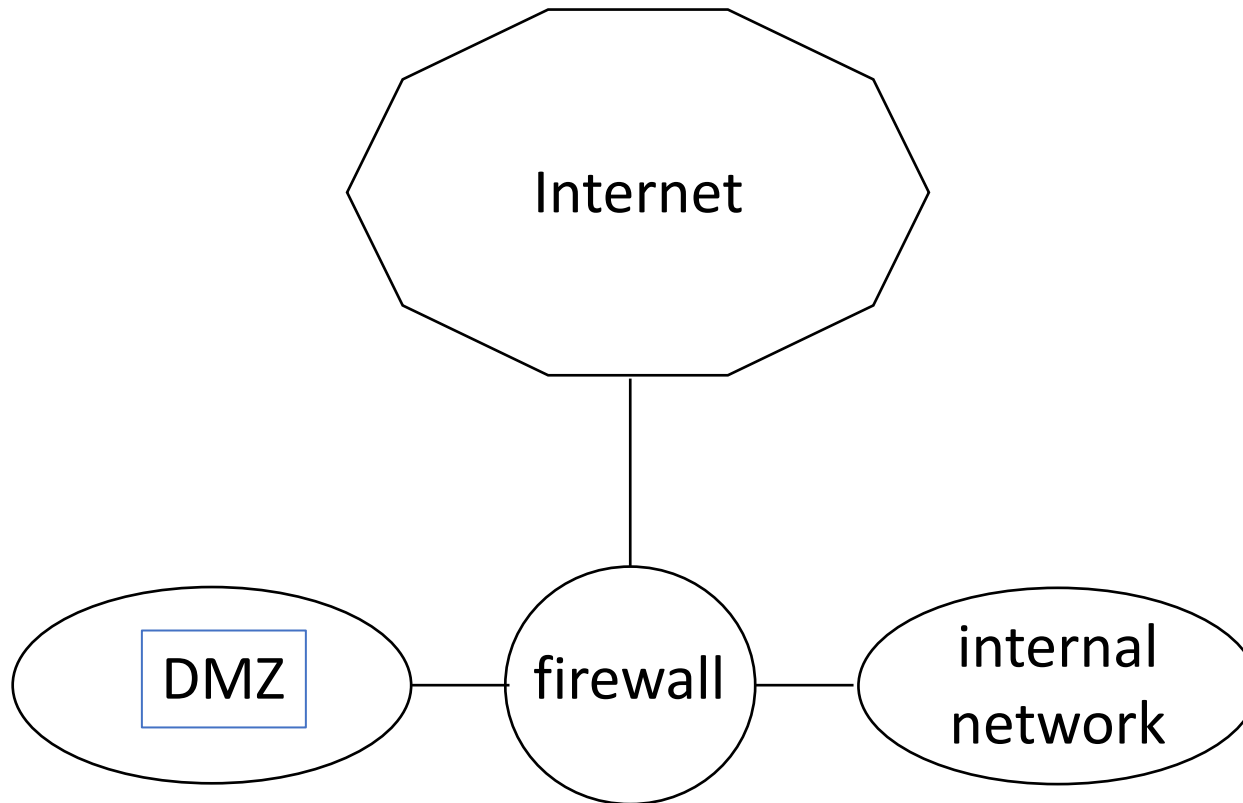
# Stateful Firewall

- Keeps track of the state of each connection
- Similar to a proxy firewall
  - No proxies involved, but this can examine contents of connections
  - Analyzes each packet, keeps track of state
  - When state indicates an attack, connection blocked or some other appropriate action taken

# Network Organization: DMZ

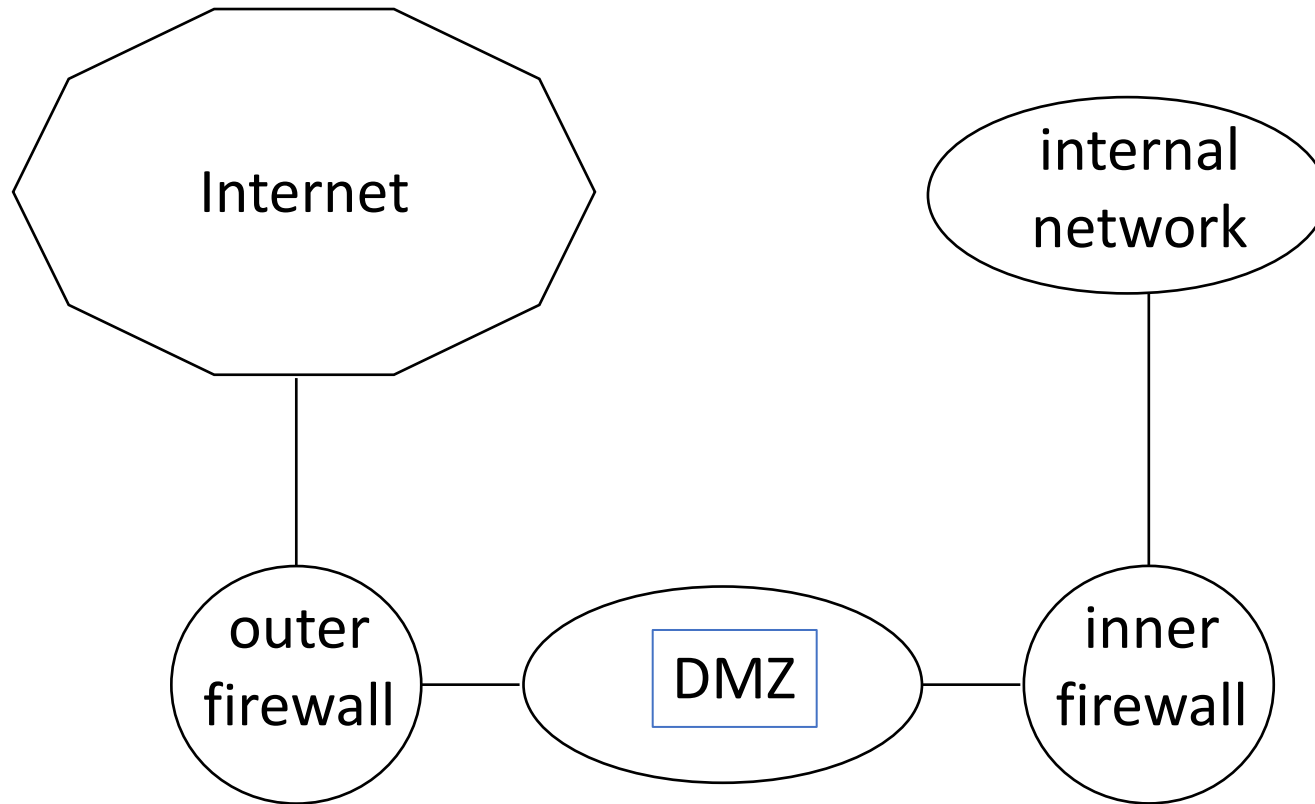
- DMZ is portion of network separating a purely internal network from external network
- Usually put systems that need to connect to the Internet here
- Firewall separates DMZ from purely internal network
- Firewall controls what information is allowed to flow through it
  - Control is bidirectional; it control flow in both directions

# One Setup of DMZ



One dual-homed firewall that routes messages to internal network or DMZ as appropriate

# Another Setup of DMZ



Two firewalls, one (outer firewall) connected to the Internet, the other (inner firewall) connected to internal network, and the DMZ is between the firewalls

# Key Points

- Both amount of information, direction of flow important
  - Flows can be explicit or implicit
- Analysis assumes lattice model
  - Non-lattices can be embedded in lattices
- Compiler-based checks flows at compile time
- Execution-based checks flows at run time
- Analysis can be for confidentiality, integrity, or both