

# $n!$ Done Recursively

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UC Davis

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

```
14:
15: int main(void)
16: {
17:     int n;
18:
19:     n = nfact(4);
20:     printf("4! is %d\n", n);
21:
22: }
```

Initial call to nfact: nfact( $n \leftarrow 4$ )

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(4): return to main, line 19  
n = 4

nfact( $n \leftarrow 4$ ):  
6: condition false, so skip  
9: call nfact(4–1), or nfact(3)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:    ↑
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(3): return to line 9, purple arrow  
 $n = 3$

nfact(4): return to main, line 19  
 $n = 4$

```
nfact(n ← 3):  
    6: condition false, so skip  
    9: call nfact(3–1), or nfact(2)
```

```
1: int nfact(int n)  
2: {  
3:     int x;  
4:  
5:     /* base case: check for 0 */  
6:     if (n == 0) return(1);  
7:  
8:     /* recurse */  
9:     x = nfact(n-1);  
10:    ↑↑  
11:    /* done! */  
12:    return(n * x);  
13: }
```

nfact(3): return to line 9, red arrow  
n = 2

nfact(3): return to line 9, purple arrow  
n = 3

nfact(4): return to main, line 19  
n = 4

```
nfact(n ← 2):  
    6: condition false, so skip  
    9: call nfact(2–1), or nfact(1)
```

```
1: int nfact(int n)  
2: {  
3:     int x;  
4:  
5:     /* base case: check for 0 */  
6:     if (n == 0) return(1);  
7:  
8:     /* recurse */  
9:     x =  nfact(n-1);  
10:  
11:    /* done! */  
12:    return(n * x);  
13: }
```

nfact(1): return to line 9, blue arrow  
n = 1

nfact(2): return to line 9, red arrow  
n = 2

nfact(3): return to line 9, purple arrow  
n = 3

nfact(4): return to main, line 19  
n = 4

nfact( $n \leftarrow 1$ ):  
6: condition false, so skip  
9: call nfact(1-1), or nfact(0)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(0): return to line 9, green arrow  
 $n = 0$

nfact(1): return to line 9, blue arrow  
 $n = 1$

nfact(2): return to line 9, red arrow  
 $n = 2$

nfact(3): return to line 9, purple arrow  
 $n = 3$

nfact(4): return to main, line 19  
 $n = 4$

nfact( $n \leftarrow 0$ ):  
6: condition true, so return 1

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(0): return to line 9, green arrow  
 $n = 0$ ; return 1

nfact(1): return to line 9, blue arrow  
 $n = 1$ ;  $nfact(0) = 1$

nfact(2): return to line 9, red arrow  
 $n = 2$

nfact(3): return to line 9, purple arrow  
 $n = 3$

nfact(4): return to main, line 19  
 $n = 4$

```

nfact(n ← 1):
    6: condition false, so skip
    9: call nfact(1–1), or nfact(0); nfact(0) = 1, so x = 1
    12: return  $1 \times 1 = 1$ 

1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =    nfact(n–1);
10:
11:    /* done! */
12:    return(n * x);
13: }

```

~~nfact(0): return to line 9, green arrow  
n = 0; return 1~~

nfact(1): return to line 9, blue arrow  
n = 1; nfact(0) = 1; return 1

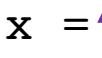
nfact(2): return to line 9, red arrow  
n = 2

nfact(3): return to line 9, purple arrow  
n = 3

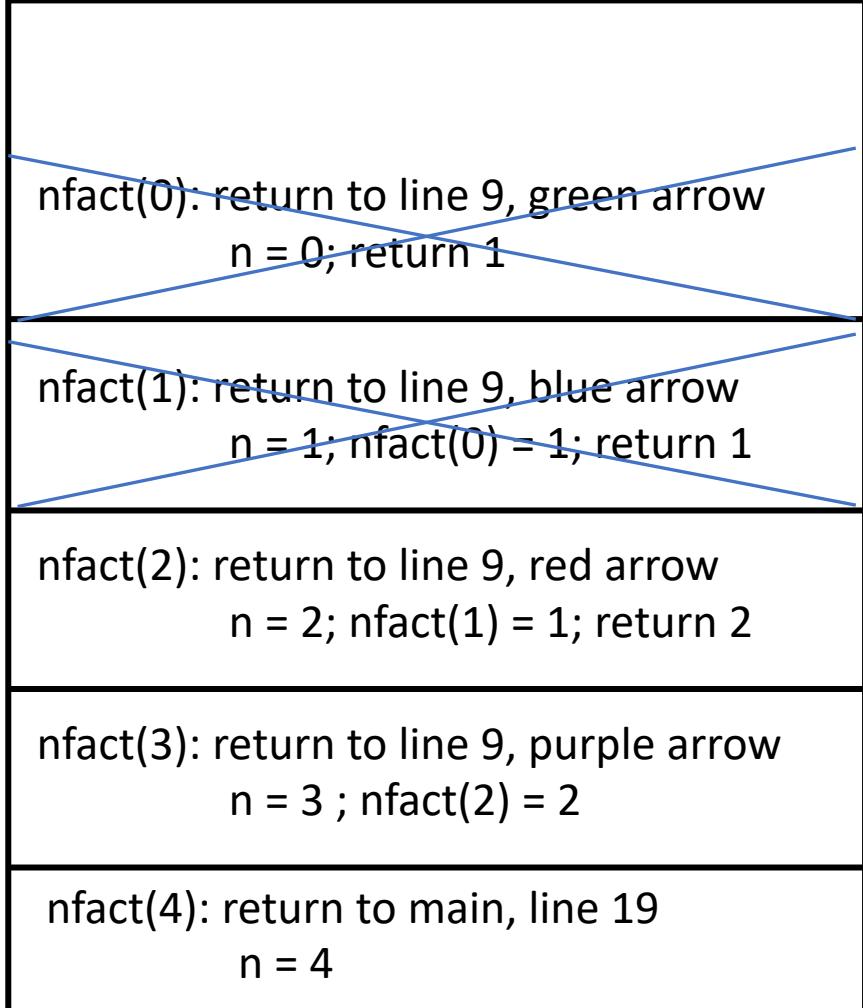
nfact(4): return to main, line 19  
n = 4

```

nfact( $n \leftarrow 2$ ):
    6: condition false, so skip
    9: call nfact(2-1), or nfact(1); nfact(1) = 1, so  $x = 1$ 
    12: return  $2 \times 1 = 2$ 

1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }

```



~~nfact(0): return to line 9, green arrow  
 $n = 0$ ; nfact(0) = 1; return 1~~

~~nfact(1): return to line 9, blue arrow  
 $n = 1$ ; nfact(0) = 1; return 1~~

~~nfact(2): return to line 9, red arrow  
 $n = 2$ ; nfact(1) = 1; return 2~~

~~nfact(3): return to line 9, purple arrow  
 $n = 3$ ; nfact(2) = 2~~

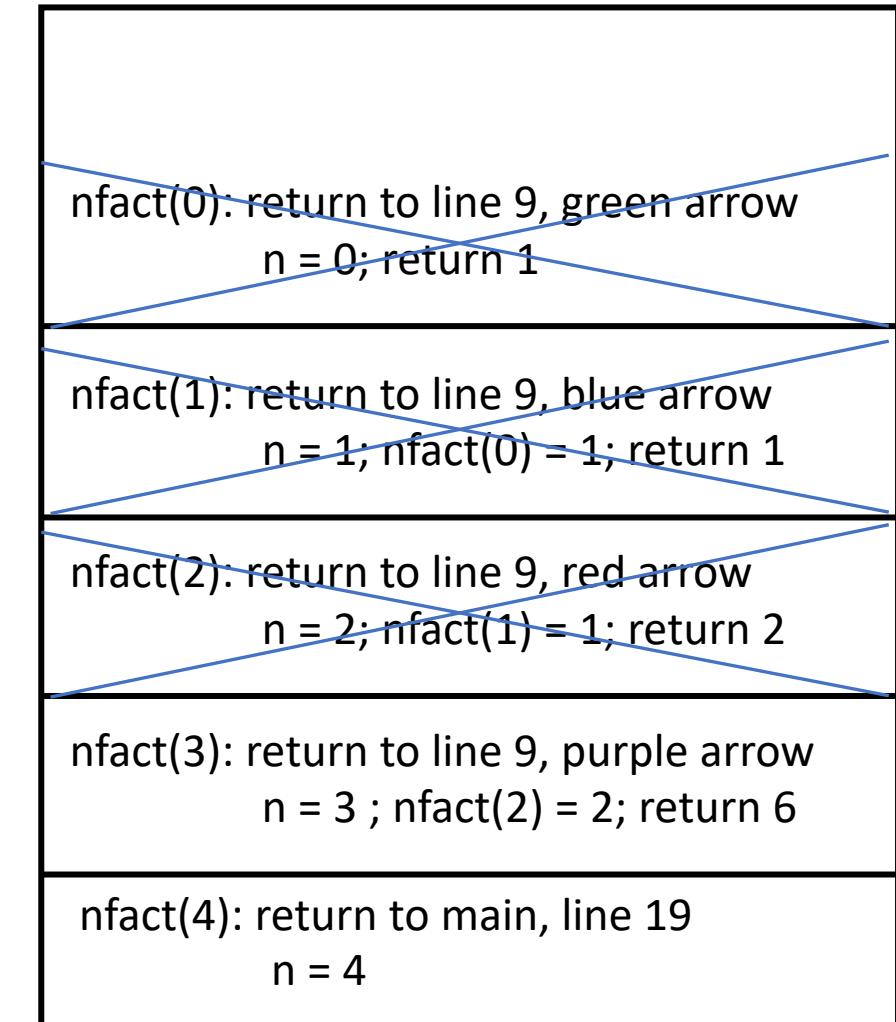
~~nfact(4): return to main, line 19  
 $n = 4$~~

```

nfact(n ← 3):
    6: condition false, so skip
    9: call nfact(3–1), or nfact(2); nfact(2) = 2, so x = 2
    12: return  $3 \times 2 = 6$ 

1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:    ↑
11:    /* done! */
12:    return(n * x);
13: }

```



```

nfact(n ← 4):
    6: condition false, so skip
    9: call nfact(4–1), or nfact(3); nfact(3) = 6, so x = 6
    12: return  $4 \times 6 = 24$ 

1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n–1);
10:    ↑
11:    /* done! */
12:    return(n * x);
13: }

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