

$n!$ Done Recursively

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```

1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
14:
15: int main(void)
16: {
17:     int n;
18:
19:     n = nfact(4);
20:     printf("4! is %d\n", n);
21:     return(0);
22: }

```

Initial call to nfact: nfact($n \leftarrow 4$)


```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(4): return to main, line 19
n = 4

nfact(n ← 4):

6: condition false, so skip

9: call nfact(4-1), or nfact(3)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```



nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 3):

6: condition false, so skip

9: call nfact(3-1), or nfact(2)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =   nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(3): return to line 9, red arrow
n = 2


nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 2):

6: condition false, so skip

9: call nfact(2-1), or nfact(1)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(1): return to line 9, blue arrow
n = 1

nfact(2): return to line 9, red arrow
n = 2


nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 1):

6: condition false, so skip

9: call nfact(1-1), or nfact(0)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(0): return to line 9, green arrow
n = 0

nfact(1): return to line 9, blue arrow
n = 1


nfact(2): return to line 9, red arrow
n = 2

nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 0):

6: condition true, so return 1

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(0): return to line 9, green arrow
n = 0; return 1

nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1

nfact(2): return to line 9, red arrow
n = 2

nfact(3): return to line 9, purple arrow
n = 3


nfact(4): return to main, line 19
n = 4

nfact(n ← 1):

6: condition false, so skip

9: call nfact(1-1), or nfact(0); nfact(0) = 1, so x = 1

12: return 1 × 1 = 1

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1

nfact(2): return to line 9, red arrow
n = 2

nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 2):

6: condition false, so skip

9: call nfact(2-1), or nfact(1); nfact(1) = 1, so x = 1

12: return 2 × 1 = 2

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = ↑↑ nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2

nfact(3): return to line 9, purple arrow
n = 3 ; nfact(2) = 2

nfact(4): return to main, line 19
n = 4

nfact(n ← 3):

6: condition false, so skip

9: call nfact(3-1), or nfact(2); nfact(2) = 2, so x = 2

12: return 3 × 2 = 6

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

~~nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2~~

nfact(3): return to line 9, purple arrow
n = 3 ; nfact(2) = 2; return 6

nfact(4): return to main, line 19
n = 4

nfact(n ← 4):

6: condition false, so skip

9: call nfact(4-1), or nfact(3); nfact(3) = 6, so x = 6

12: return 4 × 6 = 24

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

~~nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2~~

~~nfact(3): return to line 9, purple arrow
n = 3; nfact(2) = 2; return 6~~

nfact(4): return to main, line 19
n = 4; return 24