Belady's Anomaly

Introduction

Belady's anomaly demonstrates that increasing the number of page frames may also increase the number of page faults. Suppose the reference string is w = dcbadcedcbae. The page replacement algorithm is FIFO. Let us consider two memories, one with 3 frames and one with 4 frames.

| Memory With 3 F | rames | | | | | | | | | | | |
|-----------------|-------|---|---|---|---|---|---|---|---|---|----|----|
| time | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| W | d | c | b | а | d | c | e | d | c | b | а | e |
| frame 1 | d | d | d | а | а | а | e | e | e | e | e | e |
| frame 2 | | c | c | c | d | d | d | d | d | b | а | а |
| frame 3 | | | b | b | b | c | c | c | c | c | c | c |
| page fault | 1 | 2 | 3 | 4 | 5 | 6 | 7 | | | 8 | 9 | |
| page(s) loaded | d | c | b | а | d | c | e | | | b | а | |
| page(s) removed | | | | d | c | b | а | | | d | b | |
| Memory With 4 F | rames | | | | | | | | | | | |
| time | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| W | d | c | b | а | d | c | e | d | c | b | а | e |
| frame 1 | d | d | d | d | d | d | e | e | e | e | а | a |
| frame 2 | | c | c | c | c | c | c | d | d | d | d | e |
| frame 3 | | | b | b | b | b | b | b | c | c | c | c |
| frame 4 | | | | а | а | а | а | а | а | b | b | b |
| page fault | 1 | 2 | 3 | 4 | | | 5 | 6 | 7 | 8 | 9 | 10 |
| page(s) loaded | d | c | b | а | | | e | d | c | b | а | e |
| page(s) removed | | | | | | | d | c | b | а | e | а |

Analysis

The memory with 3 frames produces 9 page faults. The memory with 4 page frames produces 10 page faults.

To see why, look at the pages in memory at each time unit. At time 6, the set of pages in the 3-frame memory is not a subset of the set in the 4-frame memory. This means the 4-frame memory will producing a page fault that does not occur in the 3-frame memory. You can see this again at time 7 and time 10.

If the pages in the frames of a memory are also in the frames of a larger memory, the algorithm is said to be a *stack algorithm*. Because a stack algorithm by definition prevents the discrepancy above, no stack algorithm can suffer from Belady's anomaly.