

# Access Control Matrix

ECS 153 Spring Quarter 2021

Module 7

# Description

objects (entities)

	$O_1$	...	$O_m$	$S_1$	...	$S_n$
$S_1$						
$S_2$						
...						
$S_n$						

subjects

- Subjects  $S = \{ s_1, \dots, s_n \}$
- Objects  $O = \{ o_1, \dots, o_m \}$
- Rights  $R = \{ r_1, \dots, r_k \}$
- Entries  $A[s_i, o_j] \subseteq R$
- $A[s_i, o_j] = \{ r_x, \dots, r_y \}$  means subject  $s_i$  has rights  $r_x, \dots, r_y$  over object  $o_j$

# Example 1

- Processes  $p, q$
- Files  $f, g$
- Rights  $r, w, x, a, o$

	$f$	$g$	$p$	$q$
$p$	$rwo$	$r$	$rwxo$	$w$
$q$	$a$	$ro$	$r$	$rwxo$

# Example 2

- Host names *telegraph*, *nob*, *toadflax*
- Rights *own*, *ftp*, *nfs*, *mail*

	<i>telegraph</i>	<i>nob</i>	<i>toadflax</i>
<i>telegraph</i>	<i>own</i>	<i>ftp</i>	<i>ftp</i>
<i>nob</i>		<i>ftp, mail, nfs, own</i>	<i>ftp, nfs, mail</i>
<i>toadflax</i>		<i>ftp, mail</i>	<i>ftp, mail, nfs, own</i>

# Example 3

- Procedures *inc\_ctr*, *dec\_ctr*, *manage*
- Variable *counter*
- Rights *+*, *-*, *call*

	<i>counter</i>	<i>inc_ctr</i>	<i>dec_ctr</i>	<i>manage</i>
<i>inc_ctr</i>	<i>+</i>			
<i>dec_ctr</i>	<i>-</i>			
<i>manager</i>		<i>call</i>	<i>call</i>	<i>call</i>

# Boolean Expression Evaluation

- ACM controls access to database fields
  - Subjects have attributes
  - Verbs define type of access
  - Rules associated with objects, verb pair
- Subject attempts to access object
  - Rule for object, verb evaluated, grants or denies access

# Example

- Subject annie
  - Attributes *role* (artist), *group* (creative)
- Verb paint
  - Default 0 (deny unless explicitly granted)
- Object picture
  - Rule:  
paint: 'artist' in subject.role and  
'creative' in subject.groups and  
time.hour  $\geq 0$  and time.hour  $\leq 4$

# ACM at 3AM and 10AM

At 3AM, time condition met  
ACM is:

... picture ...

...			
annie ...		paint	

At 10AM, time condition not met  
ACM is:

... picture ...

...			
annie ...			



# State Transitions

- Change the protection state of system
- $\vdash$  represents transition
  - $X_i \vdash_{\tau} X_{i+1}$ : command  $\tau$  moves system from state  $X_i$  to  $X_{i+1}$
  - $X_i \vdash^* Y$ : a sequence of commands moves system from state  $X_i$  to  $Y$
- Commands often called *transformation procedures*

# Primitive Operations

- **create subject  $s$ ; create object  $o$** 
  - Creates new row, column in ACM; creates new column in ACM
- **destroy subject  $s$ ; destroy object  $o$** 
  - Deletes row, column from ACM; deletes column from ACM
- **enter  $r$  into  $A[s, o]$** 
  - Adds  $r$  rights for subject  $s$  over object  $o$
- **delete  $r$  from  $A[s, o]$** 
  - Removes  $r$  rights from subject  $s$  over object  $o$

# Create Subject

- Precondition:  $s \notin S$
- Primitive command: **create subject  $s$**
- Postconditions:
  - $S' = S \cup \{s\}, O' = O \cup \{s\}$
  - $(\forall y \in O') [A'[s, y] = \emptyset], (\forall x \in S') [A'[x, s] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O) [A'[x, y] = A[x, y]]$

# Create Object

- Precondition:  $o \notin O$
- Primitive command: **create object  $o$**
- Postconditions:
  - $S' = S, O' = O \cup \{o\}$
  - $(\forall x \in S') [A'[x, o] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O) [A'[x, y] = A[x, y]]$

# Add Right

- Precondition:  $s \in S, o \in O$
- Primitive command: **enter  $r$  into  $A[s, o]$**
- Postconditions:
  - $S' = S, O' = O$
  - $A'[s, o] = A[s, o] \cup \{r\}$
  - $(\forall x \in S')(\forall y \in O' - \{o\}) [A'[x, y] = A[x, y]]$
  - $(\forall x \in S' - \{s\})(\forall y \in O') [A'[x, y] = A[x, y]]$

# Delete Right

- Precondition:  $s \in S, o \in O$
- Primitive command: **delete  $r$  from  $A[s, o]$**
- Postconditions:
  - $S' = S, O' = O$
  - $A'[s, o] = A[s, o] - \{r\}$
  - $(\forall x \in S')(\forall y \in O' - \{o\}) [A'[x, y] = A[x, y]]$
  - $(\forall x \in S' - \{s\})(\forall y \in O') [A'[x, y] = A[x, y]]$

# Destroy Subject

- Precondition:  $s \in S$
- Primitive command: **destroy subject  $s$**
- Postconditions:
  - $S' = S - \{s\}, O' = O - \{s\}$
  - $(\forall y \in O') [A'[s, y] = \emptyset], (\forall x \in S') [A'[x, s] = \emptyset]$
  - $(\forall x \in S')(\forall y \in O') [A'[x, y] = A[x, y]]$

# Destroy Object

- Precondition:  $o \in O$
- Primitive command: **destroy object  $o$**
- Postconditions:
  - $S' = S, O' = O - \{ o \}$
  - $(\forall x \in S') [A'[x, o] = \emptyset]$
  - $(\forall x \in S')(\forall y \in O') [A'[x, y] = A[x, y]]$



# Creating File

- Process  $p$  creates file  $f$  with  $r$  and  $w$  permission

```
command create•file( $p$ ,  $f$ )  
    create object  $f$ ;  
    enter own into  $A[p, f]$ ;  
    enter  $r$  into  $A[p, f]$ ;  
    enter  $w$  into  $A[p, f]$ ;  
end
```

# Mono-Operational Commands

- Make process  $p$  the owner of file  $g$

**command** *make-owner*( $p, g$ )

**enter own into**  $A[p, g];$

**end**

- Mono-operational command
  - Single primitive operation in this command

# Conditional Commands

- Let  $p$  give  $q$   $r$  rights over  $f$ , if  $p$  owns  $f$   
**command**  $grant \cdot read \cdot file \cdot 1(p, f, q)$   
    **if**  $own$  **in**  $A[p, f]$   
    **then**  
        **enter**  $r$  **into**  $A[q, f];$   
    **end**
- Mono-conditional command
  - Single condition in this command

# Multiple Conditions

- Let  $p$  give  $q$   $r$  and  $w$  rights over  $f$ , if  $p$  owns  $f$  and  $p$  has  $c$  rights over  $q$

```
command grant•read•file•2( $p, f, q$ )  
  if own in  $A[p, f]$  and  $c$  in  $A[p, q]$   
  then  
    enter  $r$  into  $A[q, f]$ ;  
    enter  $w$  into  $A[q, f]$ ;  
end
```

# Copy Flag and Right

- Allows possessor to give rights to another
- Often attached to a right (called a *flag*), so only applies to that right
  - *r* is read right that cannot be copied
  - *rc* is read right that can be copied
- Is copy flag copied when giving *r* rights?
  - Depends on model, instantiation of model

# Own Right

- Usually allows possessor to change entries in ACM column
  - So owner of object can add, delete rights for others
  - May depend on what system allows
    - Can't give rights to specific (set of) users
    - Can't pass copy flag to specific (set of) users

# Attenuation of Privilege

- Principle says you can't increase your rights, or give rights you do not possess
  - Restricts addition of rights within a system
  - Usually *ignored* for owner
    - Why? Owner gives herself rights, gives them to others, deletes her rights.

# What Is “Secure”?

- Adding a generic right  $r$  where there was not one is “leaking”
  - In what follows, a right leaks if it was not present *initially*
  - Alternately: not present *in the previous state* (not discussed here)
- If a system  $S$ , beginning in initial state  $s_0$ , cannot leak right  $r$ , it is *safe with respect to the right  $r$* 
  - Otherwise it is called *unsafe with respect to the right  $r$*



# Safety Question and Basic Results

- Is there an algorithm for determining whether a protection system  $S$  with initial state  $s_0$  is safe with respect to a generic right  $r$ ?
  - Here, “safe” = “secure” for an abstract model
- Mono-operational systems: yes, there is such an algorithm
- General systems: no, there is no such algorithm
  - Proof: reduce the halting problem to the safety question
  - Proved by Harrison, Ruzzo, and Ullman; often called the HRU result
  - Says *nothing* about particular classes of systems; this is a generic result