### Lecture 16

- Policy composition approaches
- Noninterference
  - Access control matrix interpretation
- Policy composition
  - Composing noninterfering machines may not produce a noninterfering machine!

### Model

- System as state machine
  - Subjects  $S = \{ s_i \}$
  - States  $\Sigma = \{ \sigma_i \}$
  - Outputs  $O = \{ o_i \}$
  - Commands  $Z = \{ z_i \}$
  - State transition commands  $C = S \times Z$
- Note: no inputs
  - Encode either as selection of commands or in state transition commands

### Functions

- State transition function  $T: C \times \Sigma \rightarrow \Sigma$ 
  - Describes effect of executing command c in state  $\sigma$
- Output function  $P: C \times \Sigma \rightarrow O$ 
  - Output of machine when executing command c in state  $\sigma$
- Initial state is  $\sigma_0$

# Example

- Users Heidi (high), Lucy (low)
- 2 bits of state, H (high) and L (low)
  System state is (H, L) where H, L are 0, 1
- 2 commands:  $xor_0$ ,  $xor_1$  do xor with 0, 1
  - Operations affect *both* state bits regardless of whether Heidi or Lucy issues it

### Example: 2-bit Machine

- $S = \{$  Heidi, Lucy  $\}$
- $\Sigma = \{ (0,0), (0,1), (1,0), (1,1) \}$

• 
$$C = \{ xor_0, xor_1 \}$$

	Input States $(H, L)$			
	(0,0)	(0,1)	(1,0)	(1,1)
xor0	(0,0)	(0,1)	(1,0)	(1,1)
xor1	(1,1)	(1,0)	(0,1)	(0,0)

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#### Outputs and States

- *T* is inductive in first argument, as  $T(c_0, \sigma_0) = \sigma_1; T(c_{i+1}, \sigma_{i+1}) = T(c_{i+1}, T(c_i, \sigma_i))$
- Let *C*\* be set of possible sequences of commands in *C*

• 
$$T^*: C^* \times \Sigma \rightarrow \Sigma$$
 and

$$c_s = c_0 \dots c_n \Rightarrow T^*(c_s, \sigma_i) = T(c_n, \dots, T(c_0, \sigma_i) \dots)$$

• *P* similar; define *P*\* similarly

# Projection

- $T^*(c_s, \sigma_i)$  sequence of state transitions
- $P^*(c_s, \sigma_i)$  corresponding outputs
- $proj(s, c_s, \sigma_i)$  set of outputs in  $P^*(c_s, \sigma_i)$  that subject *s* authorized to see
  - In same order as they occur in  $P^*(c_s, \sigma_i)$
  - Projection of outputs for s
- Intuition: list of outputs after removing outputs that *s* cannot see

# Purge

- $G \subseteq S$ , G a group of subjects
- $A \subseteq Z$ , A a set of commands
- $\pi_G(c_s)$  subsequence of  $c_s$  with all elements  $(s,z), s \in G$  deleted
- $\pi_A(c_s)$  subsequence of  $c_s$  with all elements  $(s,z), z \in A$  deleted
- $\pi_{G,A}(c_s)$  subsequence of  $c_s$  with all elements  $(s,z), s \in G$  and  $z \in A$  deleted

### Example: 2-bit Machine

- Let  $\sigma_0 = (0,1)$
- 3 commands applied:
  - Heidi applies *xor*<sub>0</sub>
  - Lucy applies  $xor_1$
  - Heidi applies  $xor_1$
- $c_s = ((\text{Heidi}, xor_0), (\text{Lucy}, xor_1), (\text{Heidi}, xor_0))$
- Output is 011001
  - Shorthand for sequence (0,1)(1,0)(0,1)

# Example

- *proj*(Heidi,  $c_s, \sigma_0$ ) = 011001
- $proj(Lucy, c_s, \sigma_0) = 101$
- $\pi_{\text{Lucy}}(c_s) = ((\text{Heidi}, xor_0), (\text{Heidi}, xor_1))$
- $\pi_{\text{Lucy},xor1}(c_s) = ((\text{Heidi}, xor_0), (\text{Heidi}, xor_1))$
- $\pi_{\text{Heidi}}(c_s) = ((\text{Lucy}, xor_1))$

## Example

•  $\pi_{\text{Lucy},xor0}(c_s) = ((\text{Heidi}, xor_0), (\text{Lucy}, xor_1), (\text{Heidi}, xor_1))$ 

• 
$$\pi_{\text{Heidi},xor0}(c_s) = \pi_{xor0}(c_s) = ((\text{Lucy}, xor_1), (\text{Heidi}, xor_1))$$

- $\pi_{\text{Heidi, xor1}}(c_s) = ((\text{Heidi, xor}_0), (\text{Lucy, xor}_1))$
- $\pi_{xor1}(c_s) = ((\text{Heidi}, xor_0))$

#### Noninterference

- Intuition: Set of outputs Lucy can see corresponds to set of inputs she can see, there is no interference
- Formally:  $G, G' \subseteq S, G \neq G'; A \subseteq Z$ ; Users in *G* executing commands in *A* are *noninterfering* with users in *G'* iff for all  $c_s \in C^*$ , and for all  $s \in G'$ ,

$$proj(s, c_s, \sigma_i) = proj(s, \pi_{G,A}(c_s), \sigma_i)$$

– Written A,G : I G'

## Example

- Let  $c_s = ((\text{Heidi}, xor_0), (\text{Lucy}, xor_1), (\text{Heidi}, xor_1))$ and  $\sigma_0 = (0, 1)$
- Take  $G = \{ \text{Heidi} \}, G' = \{ \text{Lucy} \}, A = \emptyset$
- $\pi_{\text{Heidi}}(c_s) = ((\text{Lucy}, xor_1))$ - So *proj*(Lucy,  $\pi_{\text{Heidi}}(c_s), \sigma_0) = 0$
- proj(Lucy,  $c_s, \sigma_0$ ) = 101
- So { Heidi } : I { Lucy } is false
  - Makes sense; commands issued to change *H* bit also affect *L* bit

## Example

- Same as before, but Heidi's commands affect *H* bit only, Lucy's the *L* bit only
- Output is  $0_H 0_L 1_H$
- $\pi_{\text{Heidi}}(c_s) = ((\text{Lucy}, xor1))$ - So  $proj(\text{Lucy}, \pi_{\text{Heidi}}(c_s), \sigma_0) = 0$
- proj(Lucy,  $c_s, \sigma_0$ ) = 0
- So { Heidi } : I { Lucy } is true
  - Makes sense; commands issued to change H bit now do not affect L bit

# Security Policy

- Partitions systems into authorized, unauthorized states
- Authorized states have no forbidden interferences
- Hence a *security policy* is a set of noninterference assertions
  - See previous definition

### Alternative Development

- System X is a set of protection domains  $D = \{ d_1, \dots, d_n \}$
- When command *c* executed, it is executed in protection domain *dom*(*c*)
- Give alternate versions of definitions shown previously

### Output-Consistency

- $c \in C, dom(c) \in D$
- $\sim^{dom(c)}$  equivalence relation on states of system X
- $\sim^{dom(c)}$  output-consistent if

 $\sigma_a \sim^{dom(c)} \sigma_b \Rightarrow P(c, \sigma_a) = P(c, \sigma_b)$ 

• Intuition: states are output-consistent if for subjects in *dom*(*c*), projections of outputs for both states after *c* are the same

# Security Policy

- $D = \{ d_1, \dots, d_n \}, d_i$  a protection domain
- *r*: *D*×*D* a reflexive relation
- Then *r* defines a security policy
- Intuition: defines how information can flow around a system
  - $d_i r d_j$  means info can flow from  $d_i$  to  $d_j$  $- d_i r d_i$  as info can flow within a domain

## **Projection Function**

- $\pi'$  analogue of  $\pi$ , earlier
- Commands, subjects absorbed into protection domains
- $d \in D, c \in C, c_s \in C^*$
- $\pi'_d(\mathbf{v}) = \mathbf{v}$
- $\pi'_d(c_s c) = \pi'_d(c_s)c$  if dom(c)rd
- $\pi'_d(c_s c) = \pi'_d(c_s)$  otherwise
- Intuition: if executing *c* interferes with *d*, then *c* is visible; otherwise, as if *c* never executed

#### Noninterference-Secure

- System has set of protection domains *D*
- System is noninterference-secure with respect to policy *r* if

 $P^*(c, T^*(c_s, \sigma_0)) = P^*(c, T^*(\pi'_d(c_s), \sigma_0))$ 

• Intuition: if executing  $c_s$  causes the same transitions for subjects in domain *d* as does its projection with respect to domain *d*, then no information flows in violation of the policy

#### Lemma

- Let  $T^*(c_s, \sigma_0) \sim^d T^*(\pi'_d(c_s), \sigma_0)$  for  $c \in C$
- If ~<sup>d</sup> output-consistent, then system is noninterference-secure with respect to policy *r*

## Proof

- d = dom(c) for  $c \in C$
- By definition of output-consistent,

$$T^*(c_s, \sigma_0) \sim^d T^*(\pi'_d(c_s), \sigma_0)$$

implies

 $P^*(c, T^*(c_s, \sigma_0)) = P^*(c, T^*(\pi'_d(c_s), \sigma_0))$ 

• This is definition of noninterference-secure with respect to policy *r* 

# Unwinding Theorem

- Links security of sequences of state transition commands to security of individual state transition commands
- Allows you to show a system design is ML secure by showing it matches specs from which certain lemmata derived
  - Says *nothing* about security of system, because of implementation, operation, *etc*. issues

# Locally Respects

- *r* is a policy
- System X locally respects r if dom(c) being noninterfering with  $d \in D$  implies  $\sigma_a \sim^d T(c, \sigma_a)$
- Intuition: applying *c* under policy *r* to system *X* has no effect on domain *d* when *X* locally respects *r*

#### Transition-Consistent

- r policy,  $d \in D$
- If  $\sigma_a \sim^d \sigma_b$  implies  $T(c, \sigma_a) \sim^d T(c, \sigma_b)$ , system X transition-consistent under r
- Intuition: command *c* does not affect equivalence of states under policy *r*

#### Lemma

- $c_1, c_2 \in C, d \in D$
- For policy r,  $dom(c_1)rd$  and  $dom(c_2)rd$
- Then

 $T^*(c_1c_2,\!\sigma)=T(c_1,\!T(c_2,\!\sigma))=T(c_2,\!T(c_1,\!\sigma))$ 

• Intuition: if info can flow from domains of commands into *d*, then order doesn't affect result of applying commands

#### Theorem

- *r* policy, *X* system that is output consistent, transition consistent, locally respects *r*
- X noninterference-secure with respect to policy r
- Significance: basis for analyzing systems claiming to enforce noninterference policy
  - Establish conditions of theorem for particular set of commands, states with respect to some policy, set of protection domains
  - Noninterference security with respect to *r* follows

### Proof

- Must show  $\sigma_a \sim^d \sigma_b$  implies  $T^*(c_s, \sigma_a) \sim^d T^*(\pi'_d(c_s), \sigma_b)$
- Induct on length of  $c_s$
- Basis:  $c_s = v$ , so  $T^*(c_s, \sigma) = \sigma$ ;  $\pi'_d(v) = v$ ; claim holds
- Hypothesis:  $c_s = c_1 \dots c_n$ ; then claim holds

### Induction Step

- Consider  $c_s c_{n+1}$ . Assume  $\sigma_a \sim^d \sigma_b$  and look at  $T^*(\pi'_d(c_s c_{n+1}), \sigma_b)$
- 2 cases:
  - $dom(c_{n+1})rd$  holds
  - $dom(c_{n+1})rd$  does not hold

# $dom(c_{n+1})rd$ Holds

$$T^*(\pi'_d(c_s c_{n+1}), \sigma_b) = T^*(\pi'_d(c_s) c_{n+1}, \sigma_b)$$
  
=  $T(c_{n+1}, T^*(\pi'_d(c_s), \sigma_b))$ 

– by definition of  $T^*$  and  $\pi'_d$ 

- $T(c_{n+1}, \sigma_a) \sim^d T(c_{n+1}, \sigma_b)$ - as X transition-consistent and  $\sigma_a \sim^d \sigma_b$
- $T(c_{n+1}, T^*(c_s, \sigma_a)) \sim^d T(c_{n+1}, T^*(\pi'_d(c_s), \sigma_b))$ - by transition-consistency and IH

# $dom(c_{n+1})rd$ Holds

- $T(c_{n+1}, T^*(c_s, \sigma_a)) \sim^d T(c_{n+1}, T^*(\pi'_d(c_s)c_{n+1}, \sigma_b))$ - by substitution from earlier equality  $T(c_{n+1}, T^*(c_s, \sigma_a)) \sim^d T(c_{n+1}, T^*(\pi'_d(c_s)c_{n+1}, \sigma_b))$ - by definition of  $T^*$
- proving hypothesis

# $dom(c_{n+1})rd$ Does Not Hold

$$T^*(\pi'_d(c_s c_{n+1}), \sigma_b) = T^*(\pi'_d(c_s), \sigma_b)$$

$$- \text{ by definition of } \pi'_d$$

$$T^*(c_s, \sigma_b) = T^*(\pi'_d(c_s c_{n+1}), \sigma_b)$$

$$- \text{ by above and IH}$$

$$T(c_{n+1}, T^*(c_s, \sigma_a)) \sim^d T^*(c_s, \sigma_a)$$

$$- \text{ as } X \text{ locally respects } r, \text{ so } \sigma \sim^d T(c_{n+1}, \sigma) \text{ for any } \sigma$$

$$T(c_{n+1}, T^*(c_s, \sigma_a)) \sim^d T(c_{n+1}, T^*(\pi'_d(c_s) c_{n+1}, \sigma_b))$$

$$- \text{ substituting back}$$

• proving hypothesis

## Finishing Proof

• Take  $\sigma_a = \sigma_b = \sigma_0$ , so from claim proved by induction,

$$T^*(c_s, \sigma_0) \sim^d T^*(\pi'_d(c_s), \sigma_0)$$

By previous lemma, as X (and so ~<sup>d</sup>) output consistent, then X is noninterference-secure with respect to policy r

#### Access Control Matrix

- Example of interpretation
- Given: access control information
- Question: are given conditions enough to provide noninterference security?
- Assume: system in a particular state
  - Encapsulates values in ACM

### ACM Model

• Objects  $L = \{ l_1, ..., l_m \}$ - Locations in memory

• Values 
$$V = \{ v_1, ..., v_n \}$$

– Values that L can assume

- Set of states  $\Sigma = \{ \sigma_1, \dots, \sigma_k \}$
- Set of protection domains  $D = \{ d_1, \dots, d_j \}$

#### Functions

- value:  $L \times \Sigma \rightarrow V$ 
  - returns value v stored in location l when system in state  $\sigma$
- read:  $D \rightarrow 2^V$ 
  - returns set of objects observable from domain d
- write:  $D \rightarrow 2^V$ 
  - returns set of objects observable from domain d

### Interpretation of ACM

- Functions represent ACM
  - Subject *s* in domain *d*, object *o*
  - $-r \in A[s, o]$  if  $o \in read(d)$
  - $w \in A[s, o]$  if  $o \in write(d)$
- Equivalence relation:

 $[\sigma_a \sim^{dom(c)} \sigma_b] \Leftrightarrow [ \forall l_i \in read(d) \\ [ value(l_i, \sigma_a) = value(l_i, \sigma_b) ] ]$ 

- You can read the *exactly* the same locations in both states

# Enforcing Policy r

- 5 requirements
  - 3 general ones describing dependence of commands on rights over input and output
    - Hold for all ACMs and policies
  - -2 that are specific to some security policies
    - Hold for *most* policies

## Enforcing Policy r: First

 Output of command *c* executed in domain *dom(c)* depends only on values for which subjects in *dom(c)* have read access

$$\sigma_a \sim^{dom(c)} \sigma_b \Rightarrow P(c, \sigma_a) = P(c, \sigma_b)$$

## Enforcing Policy r: Second

If c changes l<sub>i</sub>, then c can only use values of objects in read(dom(c)) to determine new value

$$[\sigma_{a} \sim^{dom(c)} \sigma_{b} and \\ (value(l_{i}, T(c, \sigma_{a})) \neq value(l_{i}, \sigma_{a}) or \\ value(l_{i}, T(c, \sigma_{b})) \neq value(l_{i}, \sigma_{b}))] \Rightarrow \\ value(l_{i}, T(c, \sigma_{a})) = value(l_{i}, T(c, \sigma_{b}))$$

## Enforcing Policy r: Third

• If c changes  $l_i$ , then dom(c) provides subject executing c with write access to  $l_i$  $value(l_i, T(c, \sigma_a)) \neq value(l_i, \sigma_a) \Rightarrow$  $l_i \in write(dom(c))$ 

## Enforcing Policies r: Fourth

- If domain *u* can interfere with domain *v*, then every object that can be read in *u* can also be read in *v*
- So if object *o* cannot be read in *u*, but can be read in *v*; and object *o'* in *u* can be read in *v*, then info flows from *o* to *o'*, then to *v*

Let  $u, v \in D$ ; then  $urv \Rightarrow read(u) \subseteq read(v)$ 

## Enforcing Policies r: Fifth

• Subject *s* can write object *o* in *v*, subject *s'* can read *o* in *u*, then domain *v* can interfere with domain *u* 

 $l_i \in read(u) \text{ and } l_i \in write(v) \Rightarrow vru$ 

#### Theorem

- Let *X* be a system satisfying the five conditions. The *X* is noninterference-secure with respect to r
- Proof: must show X output-consistent, locally respects r, transition-consistent
  - Then by unwinding theorem, theorem holds

#### Output-Consistent

• Take equivalence relation to be ~<sup>d</sup>, first condition *is* definition of output-consistent

## Locally Respects r

- Proof by contradiction: assume  $(dom(c), d) \notin r$  but  $\sigma_a \sim^d T(c, \sigma_a)$  does not hold
- Some object has value changed by *c*:

 $\exists l_i \in read(d) [ value(l_i, \sigma_a) \neq value(l_i, T(c, \sigma_a)) ]$ 

- Condition 3:  $l_i \in write(d)$
- Condition 5: *dom*(*c*)*rd*, contradiction
- So  $\sigma_a \sim^d T(c, \sigma_a)$  holds, meaning X locally respects r

#### **Transition Consistency**

- Assume  $\sigma_a \sim^d \sigma_b$
- Must show

value $(l_i, T(c, \sigma_a)) = value(l_i, T(c, \sigma_b))$ for  $l_i \in read(d)$ 

 3 cases dealing with change that *c* makes in *l<sub>i</sub>* in states σ<sub>a</sub>, σ<sub>b</sub>

### Case 1

- $value(l_i, T(c, \sigma_a)) \neq value(l_i, \sigma_a)$
- Condition 3:  $l_i \in write(dom(c))$
- As  $l_i \in read(d)$ , condition 5 says dom(c)rd
- Condition 4 says  $read(dom(c)) \subseteq read(d)$
- As  $\sigma_a \sim^d \sigma_b$ ,  $\sigma_a \sim^{dom(c)} \sigma_b$
- Condition 2:

 $value(l_i, T(c, \sigma_a)) = value(l_i, T(c, \sigma_b))$ 

• So  $T(c, \sigma_a) \sim^{dom(c)} T(c, \sigma_b)$ , as desired

#### Case 2

- $value(l_i, T(c, \sigma_b)) \neq value(l_i, \sigma_b)$
- Condition 3:  $l_i \in write(dom(c))$
- As  $l_i \in read(d)$ , condition 5 says dom(c)rd
- Condition 4 says  $read(dom(c)) \subseteq read(d)$
- As  $\sigma_a \sim^d \sigma_b$ ,  $\sigma_a \sim^{dom(c)} \sigma_b$
- Condition 2:

 $value(l_i, T(c, \sigma_a)) = value(l_i, T(c, \sigma_b))$ 

• So  $T(c, \sigma_a) \sim^{dom(c)} T(c, \sigma_b)$ , as desired

#### Case 3

- Neither of the previous two
   *value*(l<sub>i</sub>, T(c, σ<sub>a</sub>)) = value(l<sub>i</sub>, σ<sub>a</sub>)
   *value*(l<sub>i</sub>, T(c, σ<sub>b</sub>)) = value(l<sub>i</sub>, σ<sub>b</sub>)
- Interpretation of  $\sigma_a \sim^d \sigma_b$  is: for  $l_i \in read(d)$ ,  $value(l_i, \sigma_a) = value(l_i, \sigma_b)$
- So  $T(c, \sigma_a) \sim^d T(c, \sigma_b)$ , as desired
- In all 3 cases, *X* transition-consistent

## Policies Changing Over Time

- Problem: previous analysis assumes static system
  In real life, ACM changes as system commands issued
- Example:  $w \in C^*$  leads to current state
  - cando(w, s, z) holds if s can execute z in current state
  - Condition noninterference on *cando*
  - If ¬*cando*(*w*, Lara, "write *f*"), Lara can't interfere with any other user by writing file *f*

#### Generalize Noninterference

•  $G \subseteq S$  group of subjects,  $A \subseteq Z$  set of commands, *p* predicate over elements of  $C^*$ 

• 
$$c_s = (c_1, \dots, c_n) \in C^*$$

•  $\pi''(v) = v$ 

• 
$$\pi''((c_1, ..., c_n)) = (c_1', ..., c_n')$$
  
-  $c_i' = v$  if  $p(c_1', ..., c_{i-1}')$  and  $c_i = (s, z)$  with  $s \in G$  and  $z \in A$   
-  $c_i' = c_i$  otherwise

## Intuition

- $\pi''(c_s) = c_s$
- But if *p* holds, and element of  $c_s$  involves both command in *A* and subject in *G*, replace corresponding element of  $c_s$  with empty command v
  - Just like deleting entries from  $c_s$  as  $\pi_{A,G}$  does earlier

#### Noninterference

- $G, G' \subseteq S$  groups of subjects,  $A \subseteq Z$  set of commands, *p* predicate over  $C^*$
- Users in *G* executing commands in *A* are noninterfering with users in *G'* under condition *p* iff, for all c<sub>s</sub> ∈ C\*, all s ∈ G', proj(s, c<sub>s</sub>, σ<sub>i</sub>) = proj(s, π''(c<sub>s</sub>), σ<sub>i</sub>)

  Written A,G :| G' if p

## Example

• From earlier one, simple security policy based on noninterference:

 $\forall (s \in S) \; \forall (z \in Z)$ 

 $[\{z\},\{s\}:|S \text{ if } \neg cando(w,s,z)]$ 

If subject can't execute command (the ¬*cando* part), subject can't use that command to interfere with another subject

#### Another Example

• Consider system in which rights can be passed

- pass(s, z) gives s right to execute z

$$-w_n = v_1, \dots, v_n \text{ sequence of } v_i \in C^*$$
$$-prev(w_n) = w_{n-1}; \text{ last}(w_n) = v_n$$

# Policy

• No subject *s* can use *z* to interfere if, in previous state, *s* did not have right to *z*, and no subject gave it to *s* 

$$\{ z \}, \{ s \} : | S if$$

$$[\neg cando(prev(w), s, z) \land \\ [ cando(prev(w), s', pass(s, z)) \Rightarrow \\ \neg last(w) = (s', pass(s, z)) ] ]$$

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#### Effect

- Suppose  $s_1 \in S$  can execute  $pass(s_2, z)$
- For all  $w \in C^*$ ,  $cando(w, s_1, pass(s_2, z))$  true
- Initially,  $cando(v, s_2, z)$  false
- Let  $z' \in Z$  be such that  $(s_3, z')$  noninterfering with  $(s_2, z)$

- So for each  $w_n$  with  $v_n = (s_3, z')$ ,  $cando(w_n, s_2, z) = cando(w_{n-1}, s_2, z)$ 

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#### Effect

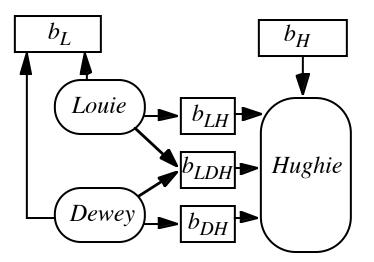
- Then policy says for all  $s \in S$   $proj(s, ((s_2, z), (s_1, pass(s_2, z)), (s_3, z'), (s_2, z)), \sigma_i)$  $= proj(s, ((s_1, pass(s_2, z)), (s_3, z'), (s_2, z)), \sigma_i)$
- So *s*<sub>2</sub>'s first execution of *z* does not affect any subject's observation of system

## Policy Composition I

- Assumed: Output function of input
  - Means deterministic (else not function)
  - Means uninterruptability (differences in timings can cause differences in states, hence in outputs)
- This result for deterministic, noninterference-secure systems

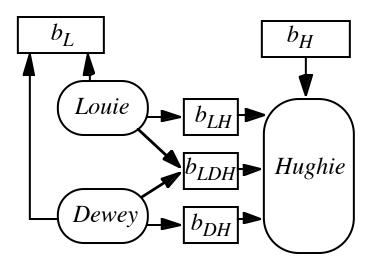
### Compose Systems

- Louie, Dewey LOW
- Hughie HIGH
- $b_L$  output buffer
  - Anyone can read it
- $b_H$  input buffer
  - From HIGH source
- Hughie reads from:
  - $b_{LH}$  (Louie writes)
  - $b_{LDH}$  (Louie, Dewey write)
  - $b_{DH}$  (Dewey writes)



#### Systems Secure

- All noninterferencesecure
  - Hughie has no output
    - So inputs don't interfere with it
  - Louie, Dewey have no input
    - So (nonexistent) inputs don't interfere with outputs



## Security of Composition

- Buffers finite, sends/receives blocking: composition *not* secure!
  - Example: assume  $b_{DH}$ ,  $b_{LH}$  have capacity 1
- Algorithm:
  - 1. Louie (Dewey) sends message to  $b_{LH} (b_{DH})$ 
    - Fills buffer
  - 2. Louie (Dewey) sends second message to  $b_{LH} (b_{DH})$
  - 3. Louie (Dewey) sends a 0 (1) to  $b_L$
  - 4. Louie (Dewey) sends message to  $b_{LDH}$ 
    - Signals Hughie that Louie (Dewey) completed a cycle

# Hughie

- Reads bit from  $b_H$ 
  - If 0, receive message from  $b_{LH}$
  - If 1, receive message from  $b_{DH}$
- Receive on  $b_{LDH}$ 
  - To wait for buffer to be filled

# Example

- Hughie reads 0 from  $b_H$ 
  - Reads message from  $b_{LH}$
- Now Louie's second message goes into  $b_{LH}$ 
  - Louie completes setp 2 and writes 0 into  $b_L$
- Dewey blocked at step 1
  - Dewey cannot write to  $b_L$
- Symmetric argument shows that Hughie reading 1 produces a 1 in  $b_L$
- So, input from  $b_H$  copied to output  $b_L$