

# January 29, 2014

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- Bell-LaPadula
  - Example Instantiation
- Tranquility
- Controversy
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# Rules, States, and Conditions

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Let  $\rho$  be a rule and  $\rho(r, v) = (d, v')$ , where  $v = (b, m, f, h)$  and  $v' = (b', m', f', h')$ . Then:

1. If  $b \subseteq b'$ ,  $f = f'$ , and  $v$  satisfies the simple security condition, then  $v'$  satisfies the simple security condition
2. If  $b \subseteq b'$ ,  $f = f'$ , and  $v$  satisfies the \*-property, then  $v'$  satisfies the \*-property
3. If  $b \subseteq b'$ ,  $m[s, o] \subseteq m'[s, o]$  for all  $s \in S$  and  $o \in O$ , and  $v$  satisfies the ds-property, then  $v'$  satisfies the ds-property

# Example Instantiation: Multics

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- 11 rules affect rights:
  - set to request, release access
  - set to give, remove access to different subject
  - set to create, reclassify objects
  - set to remove objects
  - set to change subject security level
- Set of “trusted” subjects  $S_T \subseteq S$ 
  - \*-property not enforced; subjects trusted not to violate
- $\Delta(\rho)$  domain
  - determines if components of request are valid

# *get-read* Rule

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- Request  $r = (get, s, o, \underline{r})$ 
  - $s$  gets (requests) the right to read  $o$
- Rule is  $\rho_1(r, v)$ :
  - if**  $(r \neq \Delta(\rho_1))$  **then**  $\rho_1(r, v) = (\underline{i}, v)$ ;
  - else if**  $(f_s(s) \text{ dom } f_o(o) \text{ and } [s \in S_T \text{ or } f_c(s) \text{ dom } f_o(o)])$   
**and**  $r \in m[s, o]$ 
    - then**  $\rho_1(r, v) = (y, (b \cup \{ (s, o, \underline{r}) \}, m, f, h))$ ;
  - else**  $\rho_1(r, v) = (\underline{n}, v)$ ;

# Security of Rule

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- The get-read rule preserves the simple security condition, the \*-property, and the ds-property
  - Proof
    - Let  $v$  satisfy all conditions. Let  $\rho_1(r, v) = (d, v')$ . If  $v' = v$ , result is trivial. So let  $v' = (b \cup \{ (s_2, o, \underline{r}) \}, m, f, h)$ .

# Proof

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- Consider the simple security condition.
  - From the choice of  $v'$ , either  $b' - b = \emptyset$  or  $\{ (s_2, o, \underline{r}) \}$
  - If  $b' - b = \emptyset$ , then  $\{ (s_2, o, \underline{r}) \} \in b$ , so  $v = v'$ , proving that  $v'$  satisfies the simple security condition.
  - If  $b' - b = \{ (s_2, o, \underline{r}) \}$ , because the *get-read* rule requires that  $f_c(s) \text{ dom } f_o(o)$ , an earlier result says that  $v'$  satisfies the simple security condition.

# Proof

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- Consider the \*-property.
  - Either  $s_2 \in S_T$  or  $f_c(s) \text{ dom } f_o(o)$  from the definition of *get-read*
  - If  $s_2 \in S_T$ , then  $s_2$  is trusted, so \*-property holds by definition of trusted and  $S_T$ .
  - If  $f_c(s) \text{ dom } f_o(o)$ , an earlier result says that  $v'$  satisfies the simple security condition.

# Proof

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- Consider the discretionary security property.
  - Conditions in the *get-read* rule require  $\underline{r} \in m[s, o]$  and either  $b' - b = \emptyset$  or  $\{ (s_2, o, \underline{r}) \}$
  - If  $b' - b = \emptyset$ , then  $\{ (s_2, o, \underline{r}) \} \in b$ , so  $v = v'$ , proving that  $v'$  satisfies the simple security condition.
  - If  $b' - b = \{ (s_2, o, \underline{r}) \}$ , then  $\{ (s_2, o, \underline{r}) \} \notin b$ , an earlier result says that  $v'$  satisfies the ds-property.



# *give-read* Rule

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- Request  $r = (s_1, \textit{give}, s_2, o, \underline{r})$ 
  - $s_1$  gives (request to give)  $s_2$  the (discretionary) right to read  $o$
  - Rule: can be done if giver can alter parent of object
    - If object or parent is root of hierarchy, special authorization required
- Useful definitions
  - $\textit{root}(o)$ : root object of hierarchy  $h$  containing  $o$
  - $\textit{parent}(o)$ : parent of  $o$  in  $h$  (so  $o \in h(\textit{parent}(o))$ )
  - $\textit{canallow}(s, o, v)$ :  $s$  specially authorized to grant access when object or parent of object is root of hierarchy
  - $m \wedge m[s, o] \leftarrow \underline{r}$ : access control matrix  $m$  with  $\underline{r}$  added to  $m[s, o]$

# *give-read* Rule

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- Rule is  $\rho_6(r, v)$ :  
**if**  $(r \neq \Delta(\rho_6))$  **then**  $\rho_6(r, v) = (\underline{i}, v)$ ;  
**else if**  $([o \neq \text{root}(o)$  **and**  $\text{parent}(o) \neq \text{root}(o)$  **and**  
 $\text{parent}(o) \in b(s_1:\underline{w})]$  **or**  
 $[\text{parent}(o) = \text{root}(o)$  **and**  $\text{canallow}(s_1, o, v)]$  **or**  
 $[o = \text{root}(o)$  **and**  $\text{canallow}(s_1, o, v)]$ )  
**then**  $\rho_6(r, v) = (y, (b, m \wedge m[s_2, o] \leftarrow \underline{r}, f, h))$ ;  
**else**  $\rho_1(r, v) = (\underline{n}, v)$ ;

# Security of Rule

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- The *give-read* rule preserves the simple security condition, the  $*$ -property, and the ds-property
  - Proof: Let  $v$  satisfy all conditions. Let  $\rho_1(r, v) = (d, v')$ . If  $v' = v$ , result is trivial. So let  $v' = (b, m[s_2, o] \leftarrow \underline{r}, f, h)$ . So  $b' = b, f' = f, m'[x, y] = m[x, y]$  for all  $x \in S$  and  $y \in O$  such that  $x \neq s$  and  $y \neq o$ , and  $m[s, o] \subseteq m'[s, o]$ . Then by earlier result,  $v'$  satisfies the simple security condition, the  $*$ -property, and the ds-property.

# Principle of Tranquility

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- Raising object's security level
  - Information once available to some subjects is no longer available
  - Usually assume information has already been accessed, so this does nothing
- Lowering object's security level
  - The *declassification problem*
  - Essentially, a “write down” violating \*-property
  - Solution: define set of trusted subjects that *sanitize* or remove sensitive information before security level lowered

# Types of Tranquility

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- Strong Tranquility
  - The clearances of subjects, and the classifications of objects, do not change during the lifetime of the system
- Weak Tranquility
  - The clearances of subjects, and the classifications of objects, do not change in a way that violates the simple security condition or the \*-property during the lifetime of the system

# Example of Weak Tranquility

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- Only one subject at TOP SECRET
- Document at CONFIDENTIAL
- New CONFIDENTIAL user to be added
  - User should not see document
- Raise document to SECRET
  - Subject still cannot write document
  - All security relationships unchanged

# Declassification

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- Lowering the security level of a document
  - Direct violation of the “no writes down” rule
  - May be necessary for legal or other purposes
- Declassification policy
  - Part of security policy covering this
  - Here, “secure” means classification changes to a lower level in accordance with declassification policy

# Principles

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- Principle of Semantic Consistency
- Principle of Occlusion
- Principle of Conservativity
- Principle of Monotonicity of Release



# Principle of Semantic Consistency

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- As long as the semantics of the parts of the system not involved in the declassification do not change, those parts may be changed without affecting system security
  - No leaking due to semantic incompatibilities
  - *Delimited release*: allow declassification, release of information only through specific channels (“escape hatches”)

# Principle of Occlusion

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- Declassification mechanism cannot conceal *improper* lowering of security levels
  - Robust declassification property: attacker cannot use escape hatches to obtain information unless it is properly declassified

# Other Principles

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- Principle of Conservativity
  - Absent declassification, system is secure
- Principle of Monotonicity of Release
  - When declassification is performed in an authorized manner by authorized subjects, the system remains secure

Idea: declassifying information in accordance with declassification policy does not affect security

# Controversy

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- McLean:
  - “value of the BST is much overrated since there is a great deal more to security than it captures. Further, what is captured by the BST is so trivial that it is hard to imagine a realistic security model for which it does not hold.”
  - Basis: given assumptions known to be non-secure, BST can prove a non-secure system to be secure

# †-Property

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- State  $(b, m, f, h)$  satisfies the †-property iff for each  $s \in S$  the following hold:
  1.  $b(s: \underline{a}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{a}) [f_c(s) \text{ dom } f_o(o) ] ]$
  2.  $b(s: \underline{w}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{w}) [f_o(o) = f_c(s) ] ]$
  3.  $b(s: \underline{r}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{r}) [f_c(s) \text{ dom } f_o(o) ] ]$
- Idea: for reading, subject dominates object; for writing, subject also dominates object
- Differs from \*-property in that the mandatory condition for writing is reversed
  - For \*-property, it's “object dominates subject”

# Analogues

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The following two theorems can be proved

- $\Sigma(R, D, W, z_0)$  satisfies the  $\dagger$ -property relative to  $S' \subseteq S$  for any secure state  $z_0$  iff for every action  $(r, d, (b, m, f, h), (b', m', f', h'))$ ,  $W$  satisfies the following for every  $s \in S'$ 
  - Every  $(s, o, p) \in b' - b$  satisfies the  $\dagger$ -property relative to  $S'$
  - Every  $(s, o, p) \in b$  that does not satisfy the  $\dagger$ -property relative to  $S'$  is not in  $b$
- $\Sigma(R, D, W, z_0)$  is a secure system if  $z_0$  is a secure state and  $W$  satisfies the conditions for the simple security condition, the  $\dagger$ -property, and the ds-property.

# Problem

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- This system is *clearly* non-secure!
  - Information flows from higher to lower because of the  $\dagger$ -property

# Discussion

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- Role of Basic Security Theorem is to demonstrate that rules preserve security
- Key question: what is security?
  - Bell-LaPadula defines it in terms of 3 properties (simple security condition, \*-property, discretionary security property)
  - Theorems are assertions about these properties
  - Rules describe changes to a *particular* system instantiating the model
  - Showing system is secure requires proving rules preserve these 3 properties



# Rules and Model

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- Nature of rules is irrelevant to model
- Model treats “security” as axiomatic
- Policy defines “security”
  - This instantiates the model
  - Policy reflects the requirements of the systems
- McLean’s definition differs from Bell-LaPadula
  - ... and is not suitable for a confidentiality policy
- Analysts cannot prove “security” definition is appropriate through the model

# System Z

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- System supporting weak tranquility
- On *any* request, system downgrades *all* subjects and objects to lowest level and adds the requested access permission
  - Let initial state satisfy all 3 properties
  - Successive states also satisfy all 3 properties
- Clearly not secure
  - On first request, everyone can read everything

# Reformulation of Secure Action

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- Given state that satisfies the 3 properties, the action transforms the system into a state that satisfies these properties and eliminates any accesses present in the transformed state that would violate the property in the initial state, then the action is secure
- BST holds with these modified versions of the 3 properties

# Reconsider System Z

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- Initial state:
  - subject  $s$ , object  $o$
  - $C = \{\text{High}, \text{Low}\}$ ,  $K = \{\text{All}\}$
- Take:
  - $f_c(s) = (\text{Low}, \{\text{All}\})$ ,  $f_o(o) = (\text{High}, \{\text{All}\})$
  - $m[s, o] = \{ \underline{w} \}$ , and  $b = \{ (s, o, \underline{w}) \}$ .
- $s$  requests  $\underline{r}$  access to  $o$
- Now:
  - $f'_o(o) = (\text{Low}, \{\text{All}\})$
  - $(s, o, \underline{r}) \in b'$ ,  $m'[s, o] = \{ \underline{r}, \underline{w} \}$

# Non-Secure System Z

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- As  $(s, o, \underline{r}) \in b' - b$  and  $f_o(o) \text{ dom } f_c(s)$ , access added that was illegal in previous state
  - Under the new version of the Basic Security Theorem, the current state of System Z is not secure
  - But, as  $f'_c(s) = f'_o(o)$  under the old version of the Basic Security Theorem, the current state of System Z is secure

# Response: What Is Modeling?

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- Two types of models
  1. Abstract physical phenomenon to fundamental properties
  2. Begin with axioms and construct a structure to examine the effects of those axioms
- Bell-LaPadula Model developed as a model in the first sense
  - McLean assumes it was developed as a model in the second sense

# Reconciling System Z

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- Different definitions of security create different results
  - Under one (original definition in Bell-LaPadula Model), System Z is secure
  - Under other (McLean's definition), System Z is not secure